

DUST MODELS



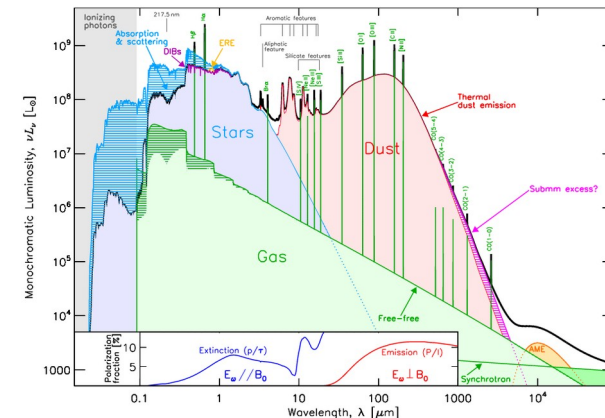
Credit: Rogelio Bernal Andreo

Dust everywhere



NGC 3190, VLT credit: ESO

- Interstellar medium less than 10% of the Milky Way mass
Dust grains make only ~1 % of that mass
Dust grains are tiny from a few Å to about $1 \mu\text{m}$
- So why bother ? Because dust is everywhere !
→ extinction of UV and visible starlight
→ emission from near-IR to microwave
- An excellent tracer of matter in galaxies
but also a major actor of its evolution

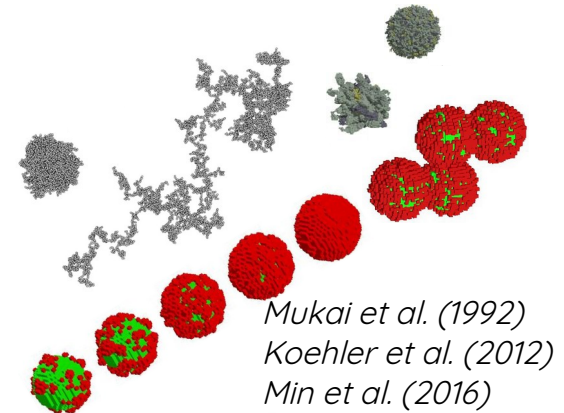


Galliano et al. (2018)

A major actor of matter evolution at all scales

- Heating of the gas by photoelectric effect
diffuse ISM ($A_V < 1$) & photon-dominated regions (PDRs)
- H_2 formation only possible on the grain surfaces
initiates all interstellar chemistry
- Determines if a cloud is optically thin or thick
Molecules protected from photodissociation
Reduced ionisation fraction
Gas cooling through collisions
- Tracer for cloud masses & magnetic field

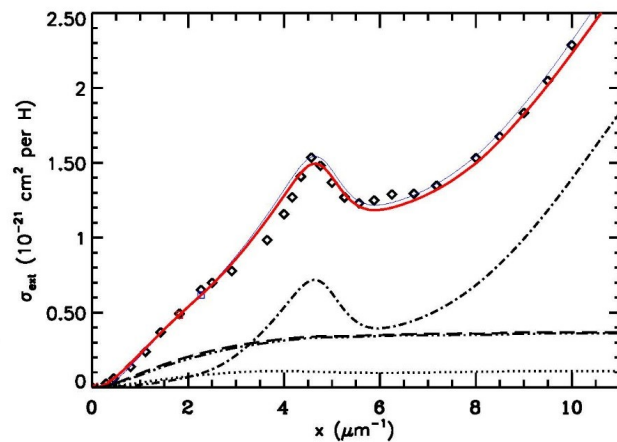
star formation



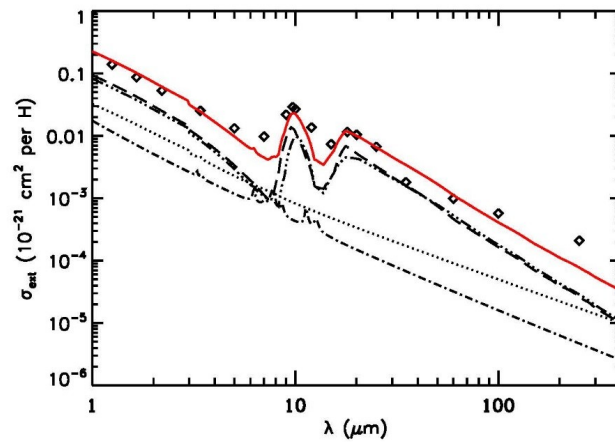
➔ *All the above processes depend upon the exact grain size, structure, composition, shape and mass*

Dust basics: extinction & emission

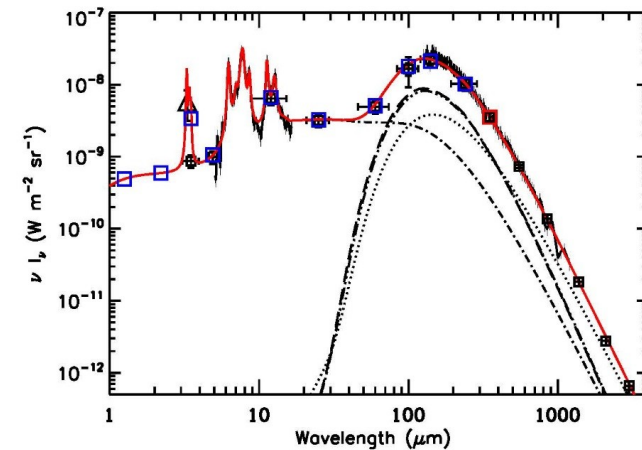
IR-vis-UV extinction



NIR-FIR extinction

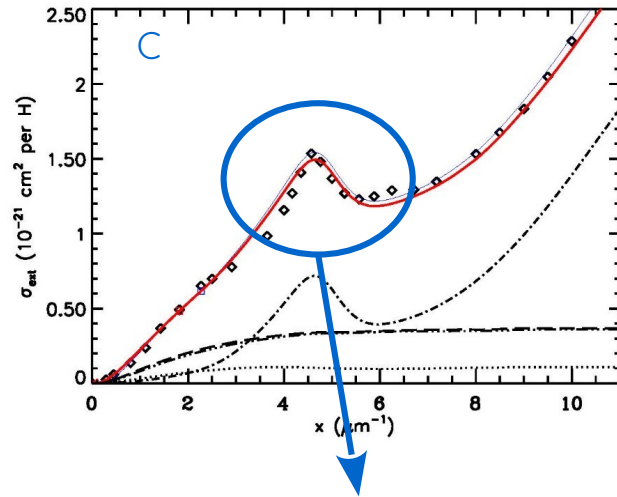


NIR-submm SED



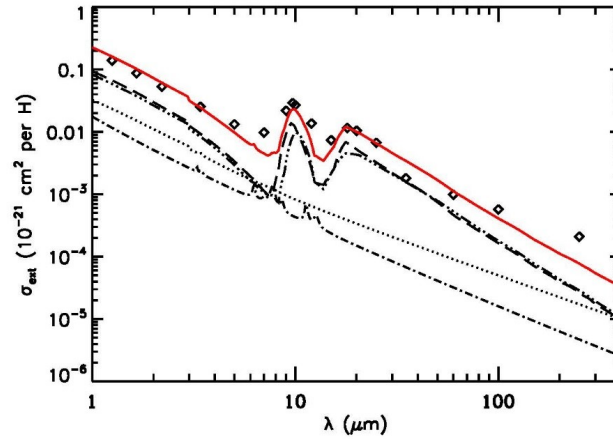
Dust basics: extinction & emission

IR-vis-UV extinction

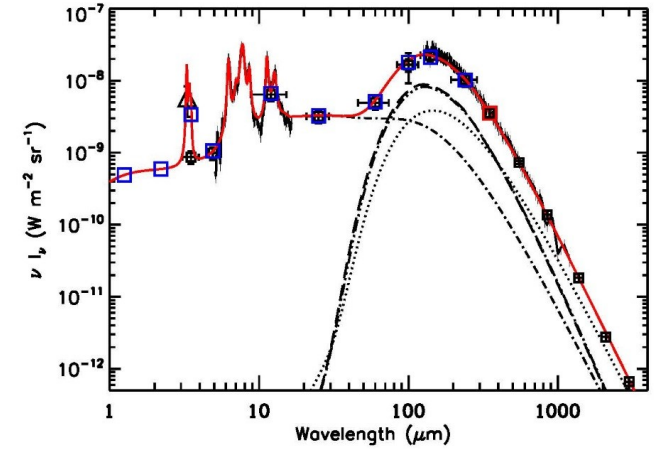


small carbonaceous particles

NIR-FIR extinction

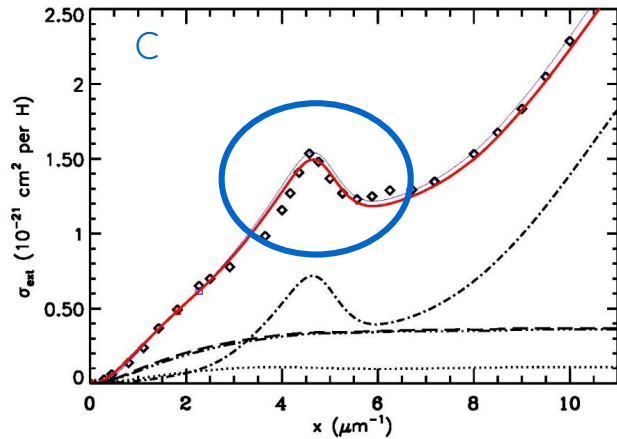


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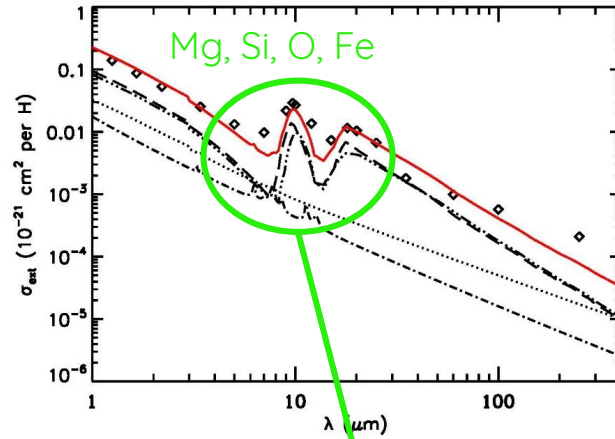


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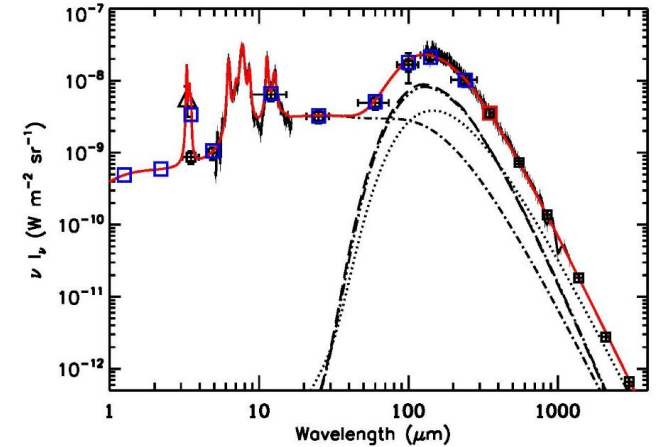
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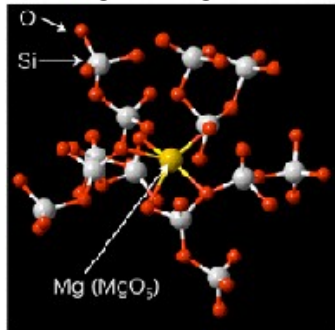
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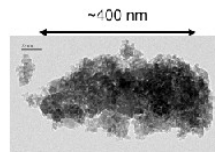


MgSiO₃ glass

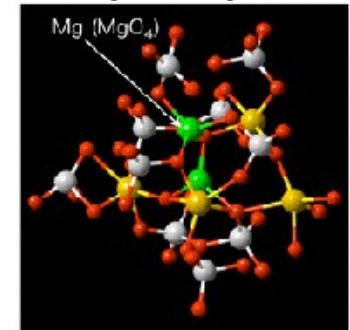


~ 9.7 and 18 microns features
amorphous silicates

normative compositions of olivine & pyroxene
Mg₂SiO₄ & MgSiO₃
with metallic iron inclusions

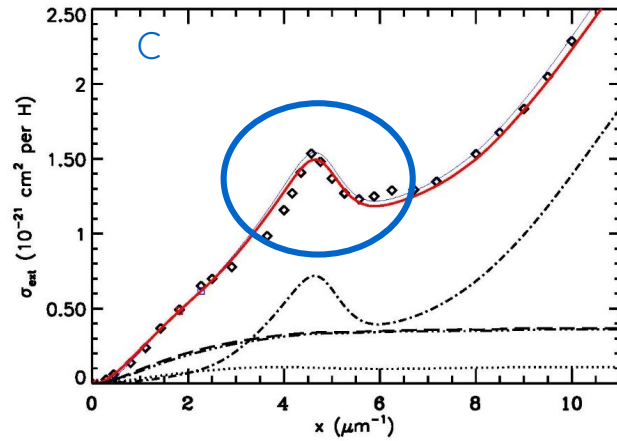


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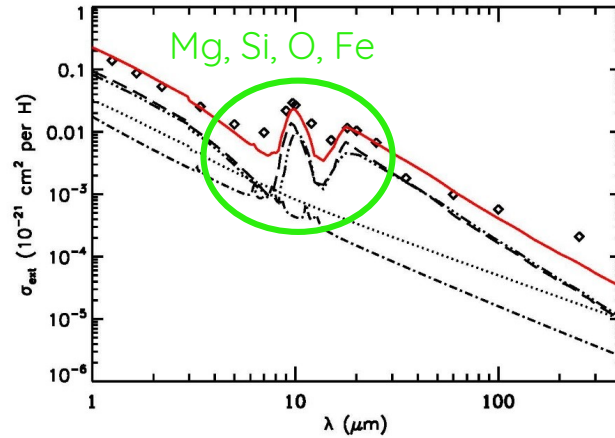


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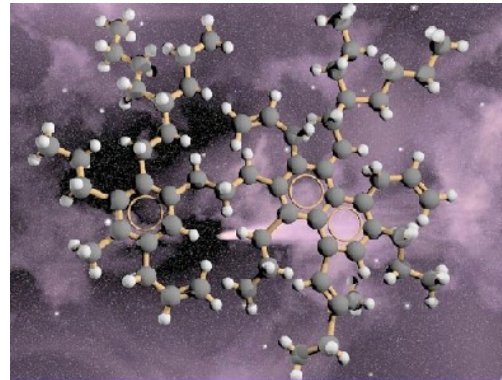
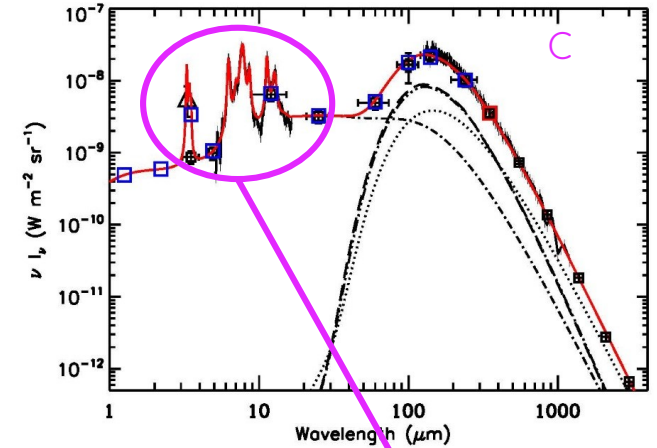
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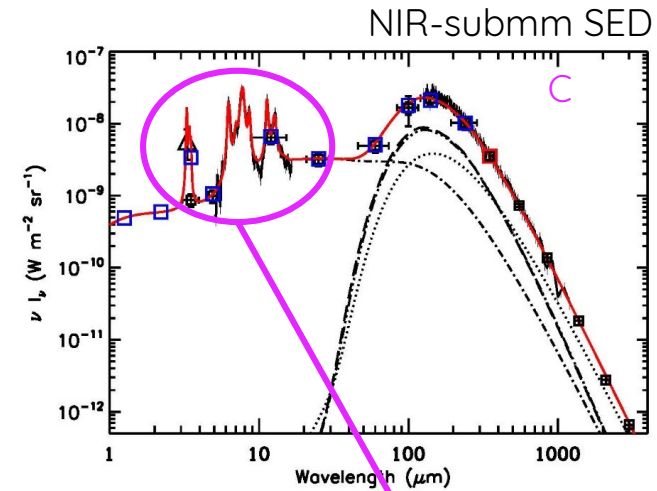
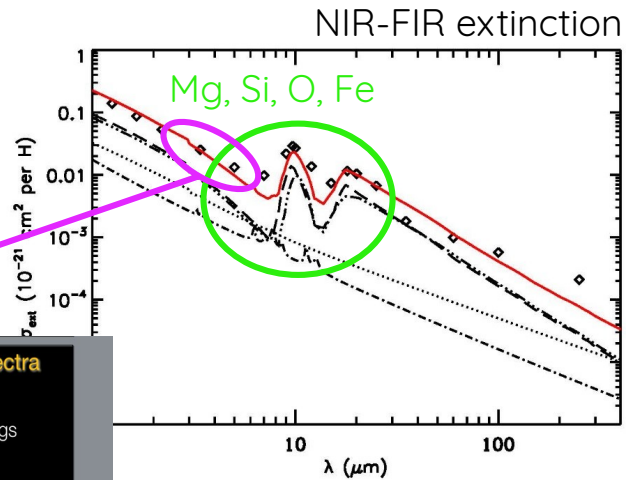
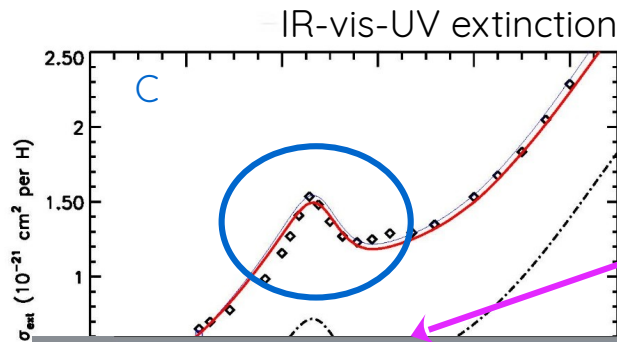


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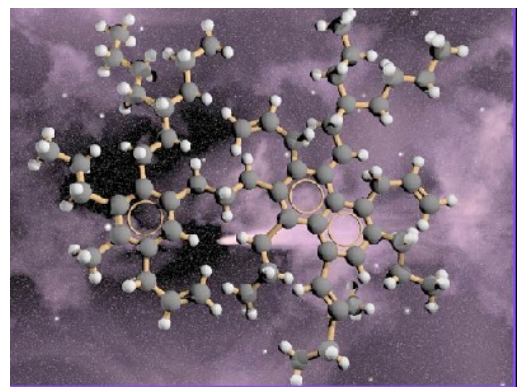
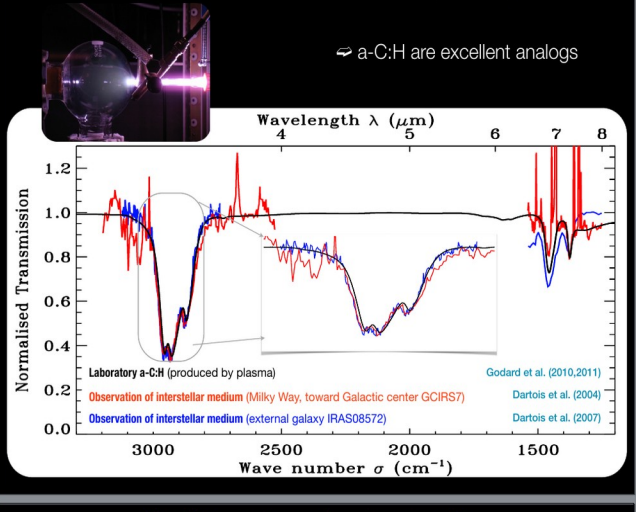
C-C and C-H on aromatic rings
 on aliphatic chains
 on olefinic bonds

Dust basics: extinction & emission



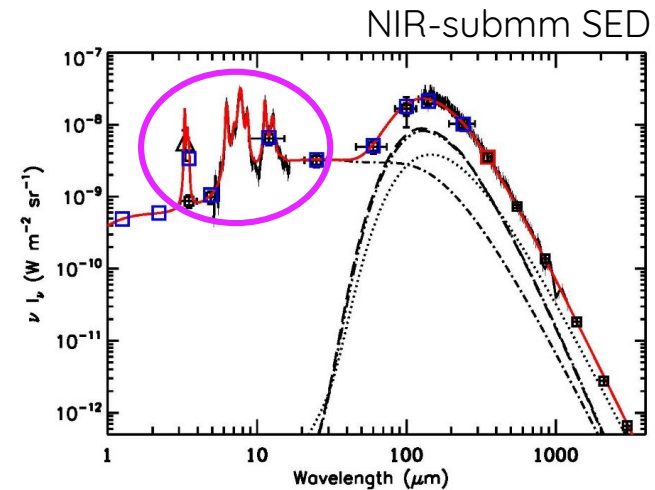
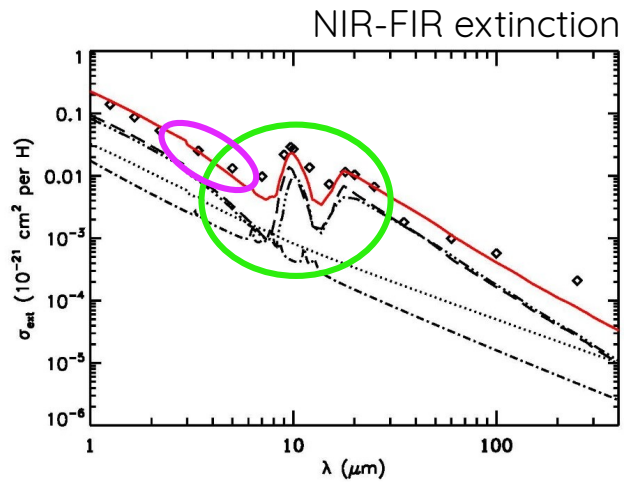
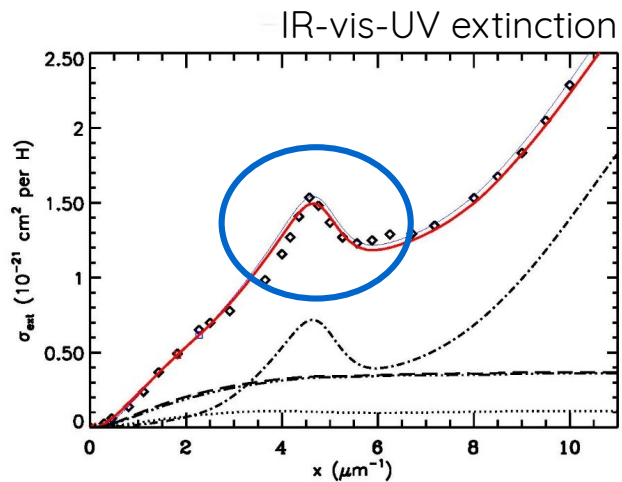
Courtesy of M. Godard (ISMO)

Comparison of observations with laboratory analogs spectra



C-C and C-H on aromatic rings
on aliphatic chains
on olefinic bonds

Dust basics: extinction & emission



emission from NIR to submm

grains have different temperatures

grains have different sizes

Dust basics: extinction & emission



$$I(\lambda) = I_0(\lambda) e^{-\tau_\lambda}$$

optical depth

$$A(\lambda) = 1.086 \tau_\lambda$$

extinction

↳ depends on the grain composition, structure, and size

For spherical particles with radius a , one can define extinction cross-sections:

$$\sigma_{\text{ext}} = \sigma_{\text{abs}} + \sigma_{\text{sca}}$$

$$\sigma_{\text{abs}} = \pi a^2 Q_{\text{abs}} \quad \& \quad \sigma_{\text{sca}} = \pi a^2 Q_{\text{sca}}$$

absorption & scattering efficiencies

complex refractive index

{
 Mie theory
 Effective medium theory
 Discrete dipole approximation, etc.

🔗 Tazaki & Tanaka (2018)

🔗 Ysard et al. (2018)

Dust basics: extinction & emission

Grain heating: absorption of UV/visible photons

Grain cooling: thermal emission of IR photons

Spherical grains of radius a illuminated by a radiation field density u_ν

$$E_{\text{abs}} = \int_0^\infty 4\pi a^2 Q_{\text{abs}}(\nu) \pi \frac{c u_\nu}{4\pi} d\nu$$

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The diagram shows the equation $E_{\text{abs}} = \int_0^\infty 4\pi a^2 Q_{\text{abs}}(\nu) \pi \frac{c u_\nu}{4\pi} d\nu$ with three arrows pointing to specific parts of the equation:

- A blue arrow points from the text "grain surface" to the term $4\pi a^2$.
- A green arrow points from the text "energy absorbed per surface unit" to the term $Q_{\text{abs}}(\nu)$.
- A red arrow points from the text "flux per steradian" to the term $\frac{c u_\nu}{4\pi}$.

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Emitted energy by a grain at temperature T

$$E_{\text{em}} = \int_0^\infty 4\pi a^2 Q_{\text{abs}}(\nu) \pi B_\nu(T) d\nu$$

Dust basics: extinction & emission

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→ grain surface
→ energy absorbed per surface unit
← flux per steradian

Emitted energy by a grain at temperature T

$$E_{\text{ém}} = \int_0^\infty 4\pi a^2 Q_{\text{abs}}(\nu) \pi B_\nu(T) d\nu$$

→ power emitted per frequency unit
← Planck function

$$E_{\text{abs}} = E_{\text{ém}} \longrightarrow T_{\text{éq}}$$

- 🔍 Lèger et al. (1989)
- 🔍 Draine & Li (2001)
- 🔍 Krügel (2002)
- 🔍 Lequeux (2002, 2005)

Dust basics: extinction & emission

small grains → weak heat capacity

at first order $E_{\text{therm}} \sim 3N_{\text{at}}k_B T$

$$C(T) \sim 3N_{\text{at}}k_B$$



one UV photon → quick and high T increase

$$T \sim h\nu / 3N_{\text{at}}k_B$$

$$30 \text{ atoms } (\sim 0.5\text{nm}) + \langle h\nu \rangle = 8\text{eV} \Rightarrow \sim 1000\text{K!}$$



quick cooling until the next absorption event

strong temperature fluctuations if $h\nu_m > \int_0^{T_{\text{eq}}} C(T) dT$

starting from T_0 $h\nu = \int_{T_0}^T C(T) dT$

cooling as $\frac{dT}{dt} = \frac{1}{C(T)} \int_0^\infty 4\pi a^2 Q_{\text{abs}}(\nu) \pi B_\nu(T) d\nu$

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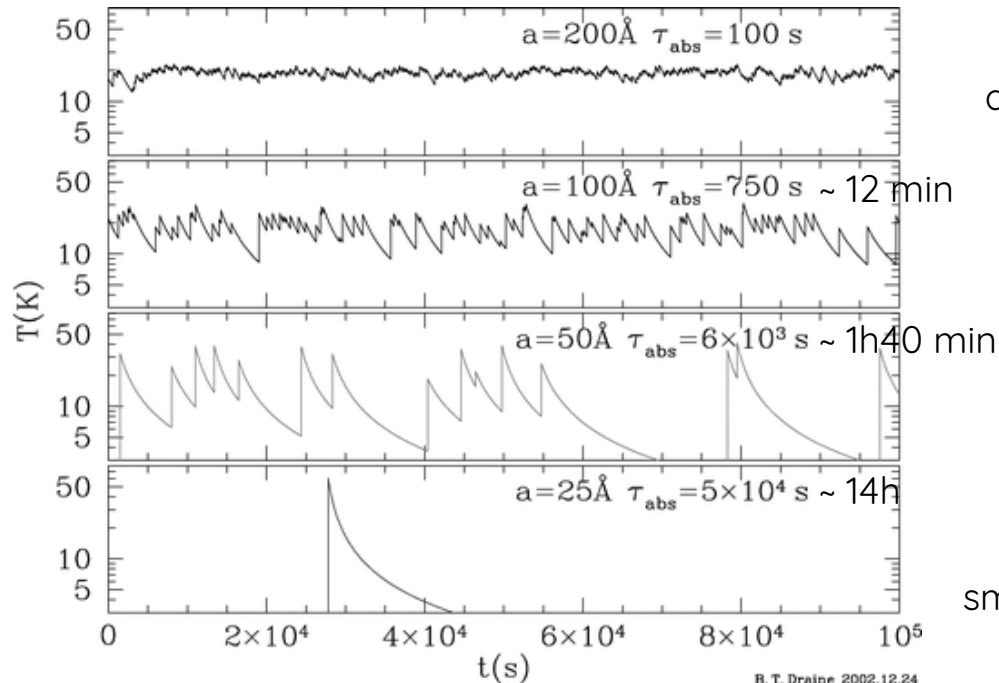
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quick cooling until the next absorption event



B. T. Draine 2002.12.24

smallest hydrocarbons ~ 1 year

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small grain emission



$$E_{\text{ém}}(\nu) = \int_0^\infty 4\pi a^2 Q_{\text{abs}}(\nu) \pi B_\nu(T) \frac{dP}{dT} dT$$

🔍 Lèger et al. (1989)

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🔍 Lequeux (2002, 2005)

Basics of all dust models

- Chemical composition
 - $m = n + ik$: from the lab ? empirical ?
 - composite grains ?
 - inclusions, ice mantles ?
- Structure
 - compact vs. porous
 - core/mantle
 - single grains vs. aggregates
 - spheres vs. spheroids vs. irregular grains

Absorption efficiency $Q_{\text{abs}}(\alpha, \lambda, T?)$
Scattering efficiency $Q_{\text{sca}}(\alpha, \lambda)$
Scattering phase function $g(\alpha, \lambda)$
Heat capacity $C(\alpha, T)$

non-trivial step

- Size distribution
 - $\alpha_{\text{min}}, \alpha_{\text{max}}$
 - log-normal, power-law, MRN, weird ?

Calculation of the optical properties: how ?

- Compact spherical grains
Compact spherical grains with mantles

Mie: BHMIE
BHCOAT

[🔍 Van de Hulst \(1957\), Bohren & Huffman \(1983\)](#)

- Porous grains
Composite grains → random distribution

Effective Medium Theory (EMT)
Maxwell Garnett or Bruggeman

[🔍 Van de Hulst \(1957\), Bohren & Huffman \(1983\)](#)

- Aggregates with one-point contact

T-MATRIX

[🔍 Mishenko \(2000\)](#)

- Aggregates with contact surface area
Grains of any shape
Composite/porous grains → controlled distribution

Discrete Dipole Approximation (DDA)

[🔍 Draine & Flatau \(1994\), Yurkin & Hoekstra \(2011\)](#)

- Spheroidal grains with or without mantles

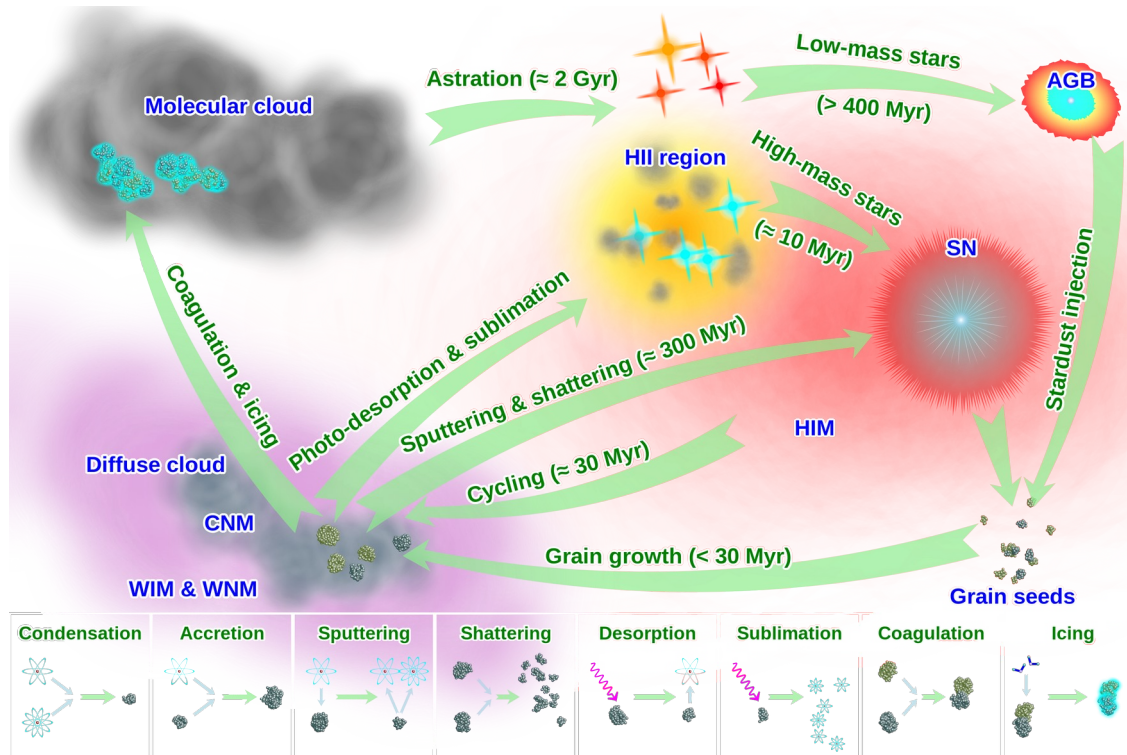
DDA, T-MATRIX

Analytical function in the Rayleigh limit

Geometric limit in the UV

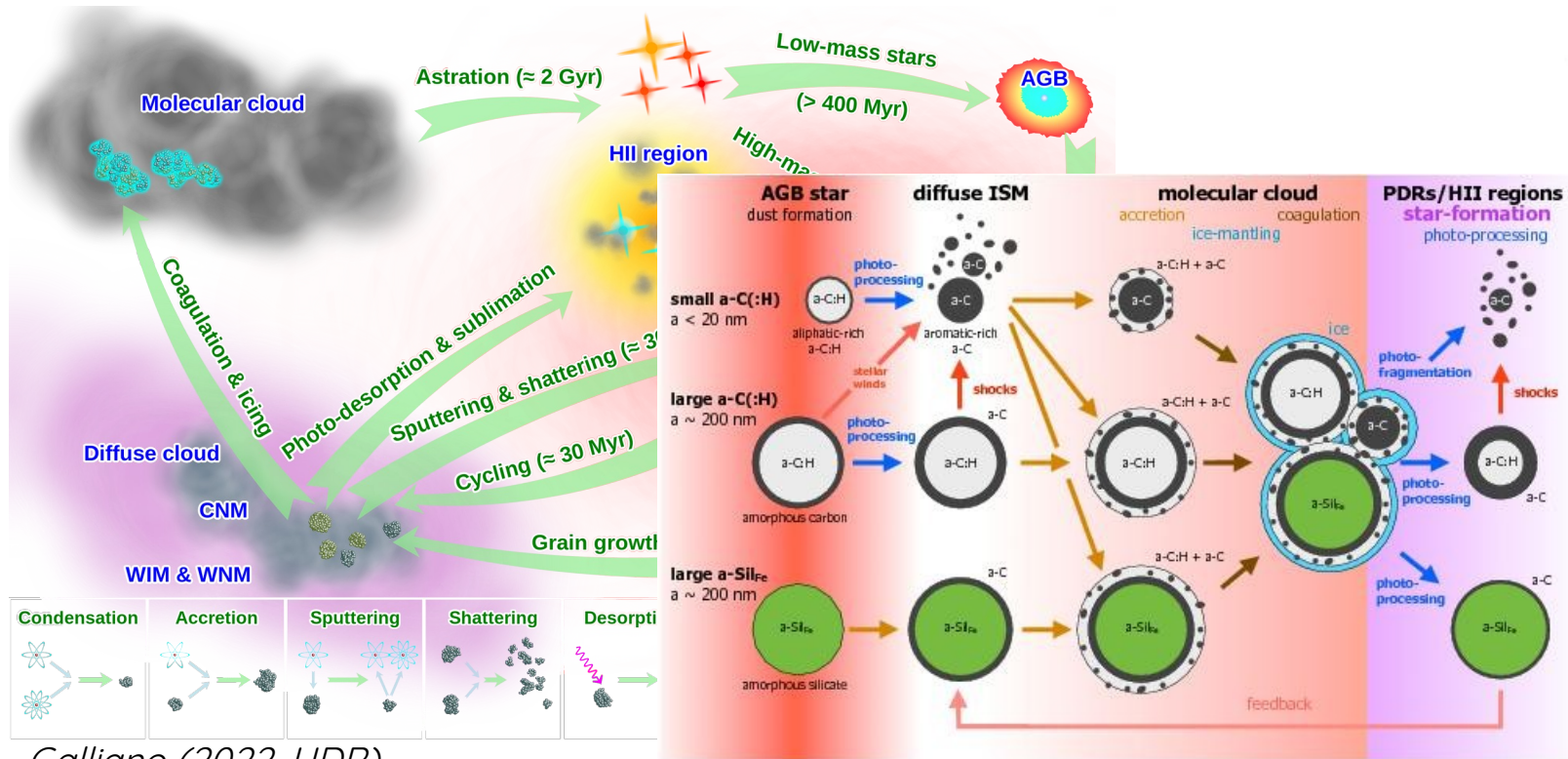
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Lifecycle of interstellar dust: a restless journey



Galliano (2022, HDR)

Lifecycle of interstellar dust: a restless journey



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Jones et al. (2013)

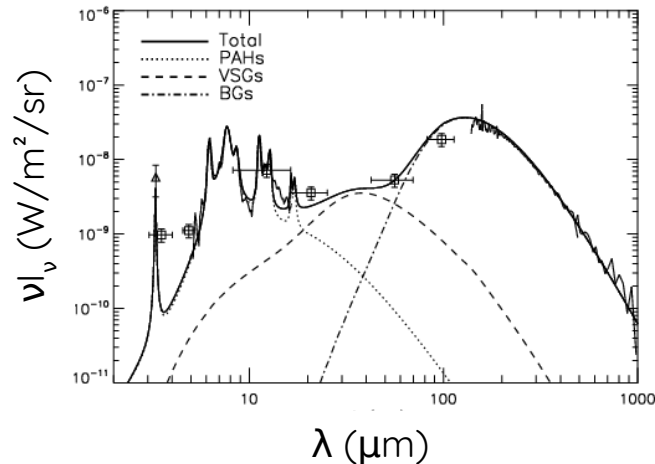
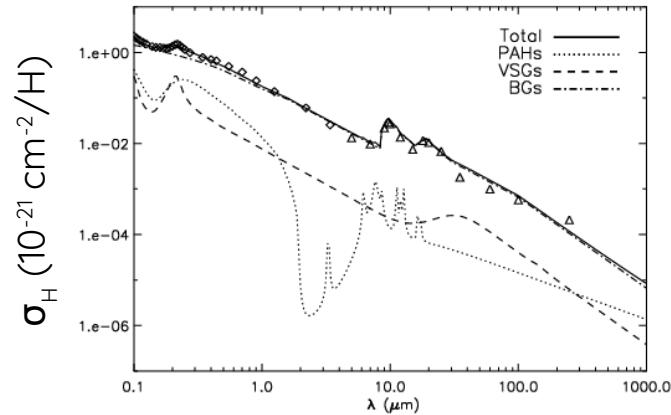
Summary

- What should a Galactic dust model fit ?
 - observations of the diffuse ISM
 - observations of the dense ISM
 - observations of PDRs
- Dust models: 2 public examples
 - an empirical model
 - a lab-based model
- A few points to bear in mind when using dust models
 - uncertainties in models
 - grain size determination
 - cloud mass estimate

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What do we have to constrain the grain properties ?



- Depletion measurements + X-ray \rightarrow composition

- Extinction

$$E(B-V) = A_B - A_V \quad \& \quad R_V = A_V / E(B-V)$$

mid-IR silicate bands at ~ 10 and $18 \mu\text{m}$

- Emission

mid-IR to far-IR ratio

$$\text{modified BB fit} \rightarrow I_\nu = N_H \sigma_{\nu 0} B_\nu(T) (\nu/\nu_0)^\beta$$

$$\text{optical depth} \rightarrow \tau_{\nu 0} = N_H \sigma_{\nu 0}$$

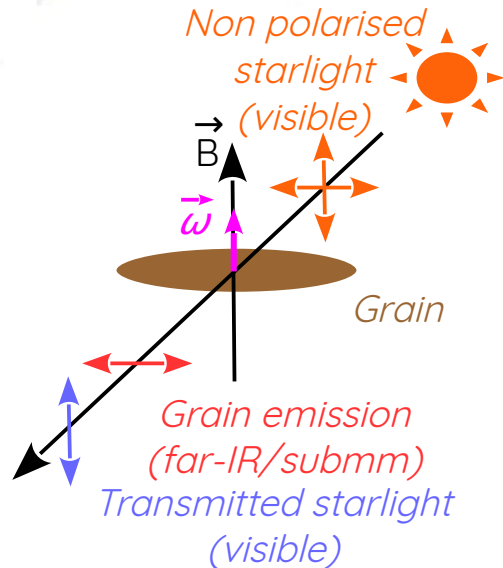
- Scattered light from visible to mid-IR \rightarrow size

- Polarisation

λ_{max} \rightarrow peak wavelength of starlight polarisation

P/I \rightarrow polarisation fraction in far-IR/submm

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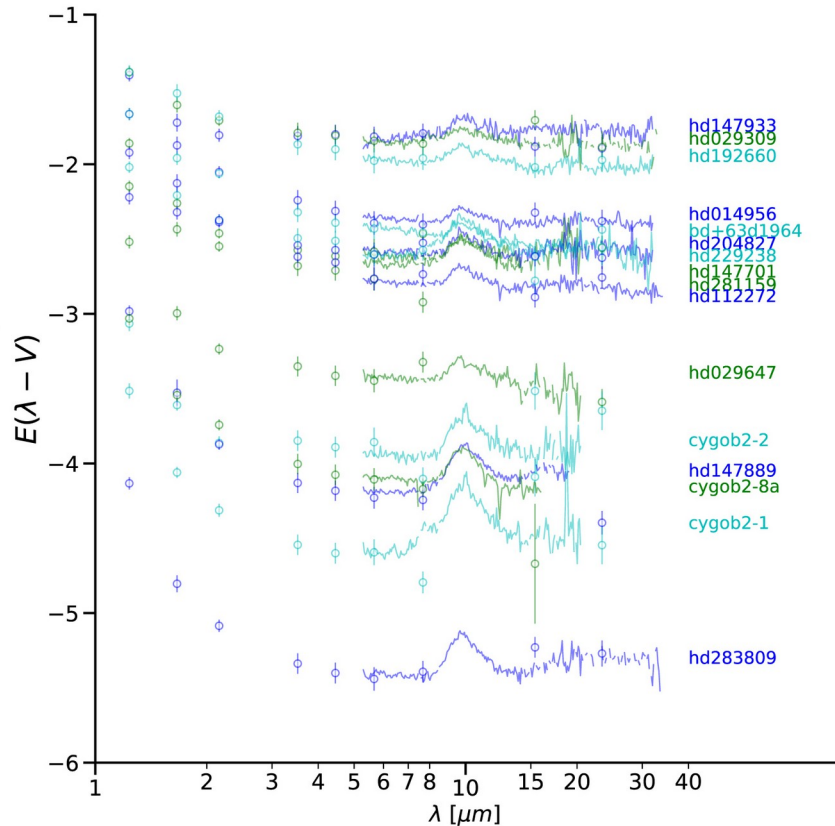
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➔ Grain composition, abundance, size, shape, structure...

What should a dust model fit for the diffuse ISM ?

Variations in the extinction curve

Gordon et al. (2021), Declair et al. (2022)



$A(V) < 3$

- 16 reddened stars Spitzer IRS spectra
- Silicate band-to-continuum ratio increases with increasing $A(V)$
- Small variations in the near-IR (IRTF SpeX)

Variation in grain size distributions ?

Iron nano-inclusions vs. Fe^{2+} in the silicate matrix ?

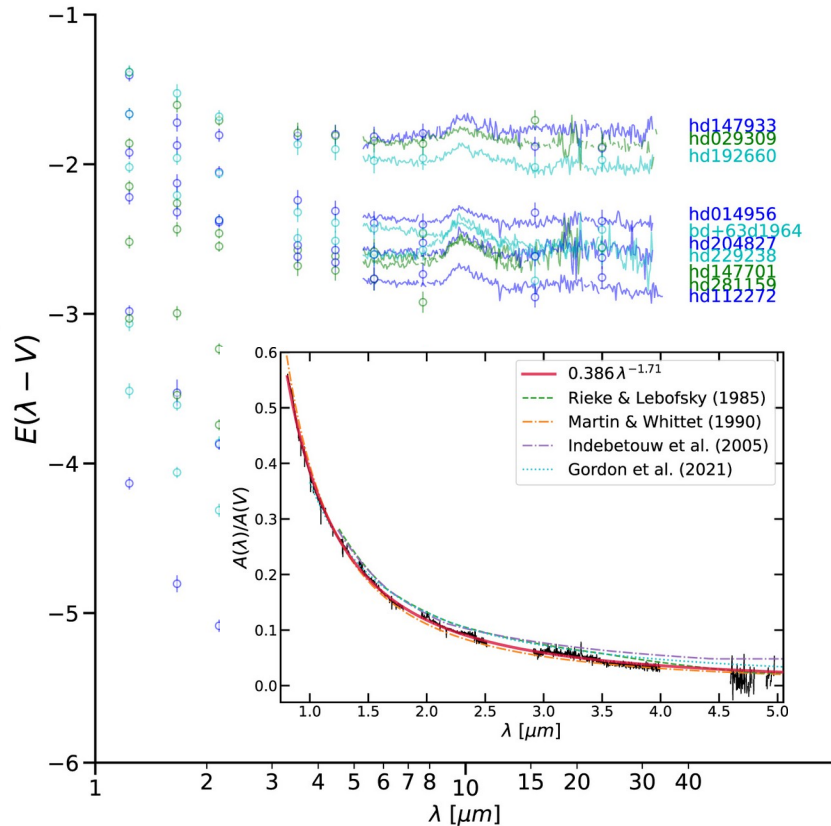
Different silicate/carbon mixing ?

Different grain shapes ?

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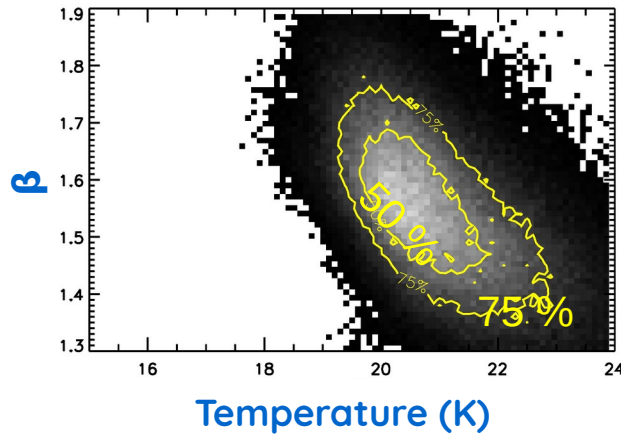
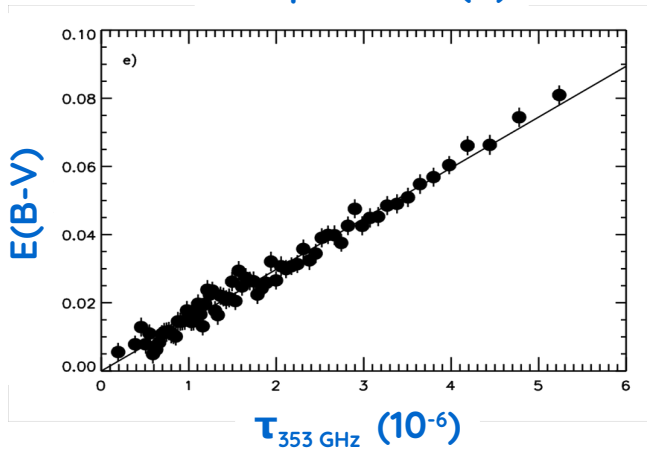
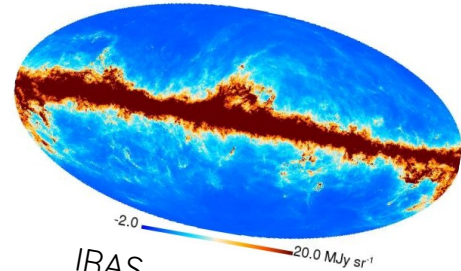
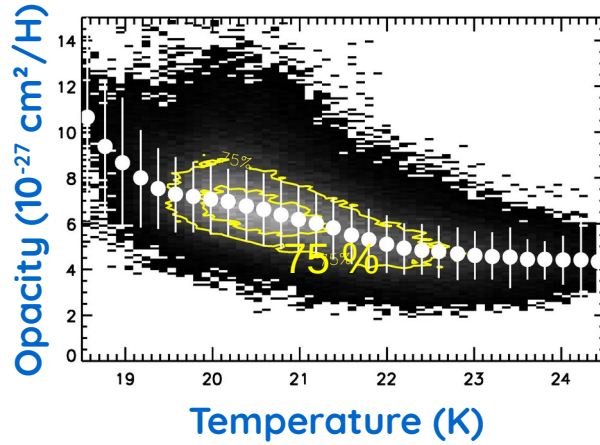
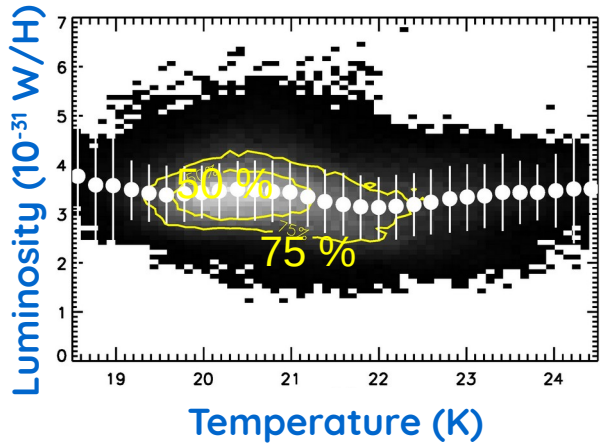
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All-diffuse-sky variations in the dust properties

Planck Collaboration XI (2014): $N_H < 3 \times 10^{20} \text{ H/cm}^2$



$$I_\nu = N_H \sigma_{\nu 0} B_\nu(T) (\nu/\nu_0)^\beta$$

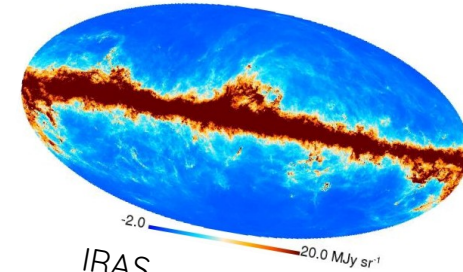
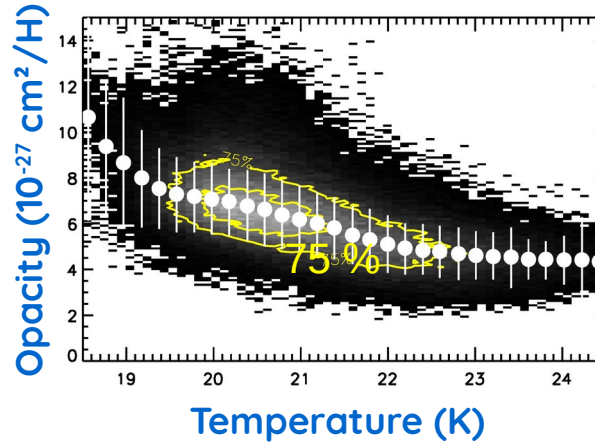
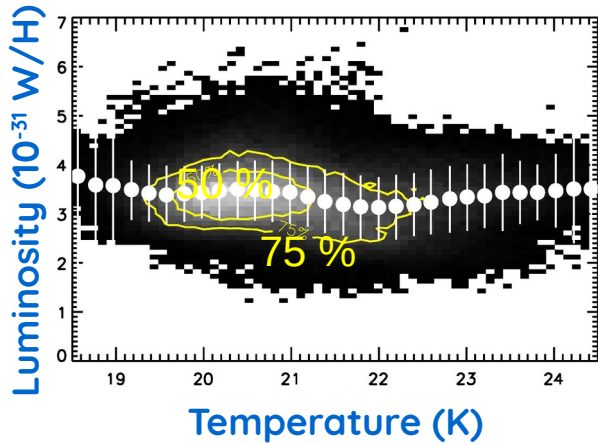
$$L_H = \int I_\nu d\nu / N_H$$

$$\tau_{\nu 0} = N_H \sigma_{\nu 0}$$

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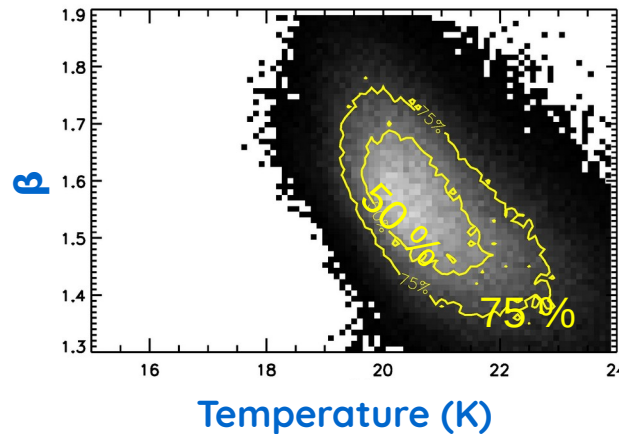
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IRAS
Planck-HFI
- 100 μm
- 350 μm
- 550 μm
- 850 μm

- $N_H < 3 \times 10^{20} \text{ H/cm}^2$
- $E(B-V)$ from SDSS data towards quasars
- Observational results
 - β -T variations
 - luminosity independent of T
 - hotter grains = less emissive grains



$$I_\nu = N_H \sigma_{\nu 0} B_\nu(T) (\nu/\nu_0)^\beta$$

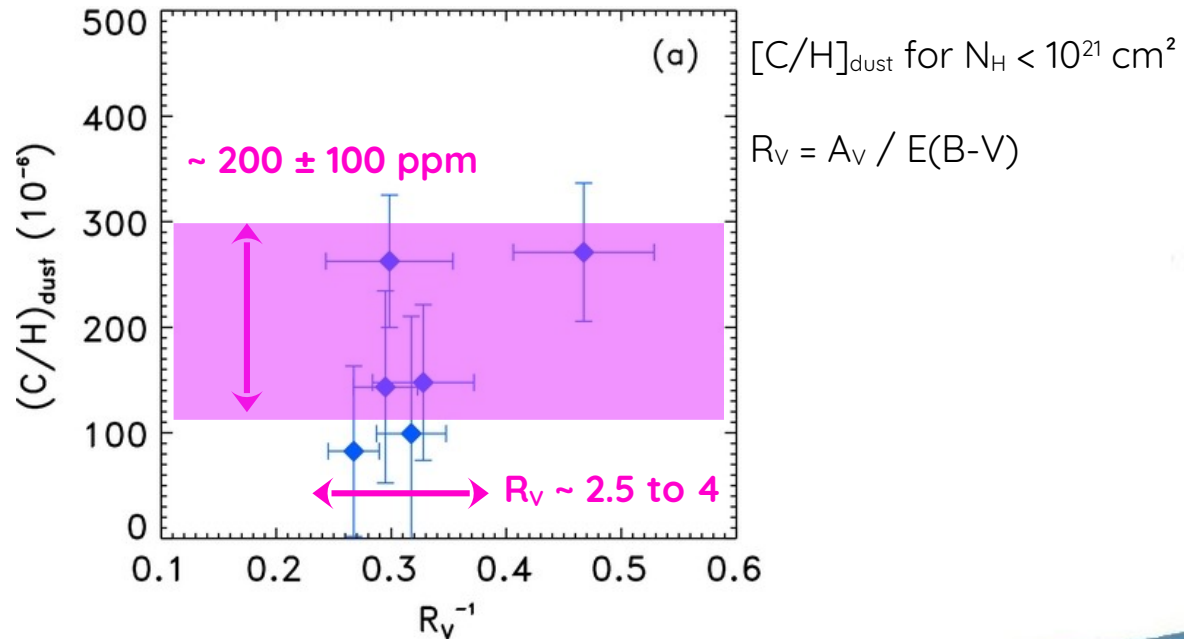
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Carbon depletion in the diffuse ISM

Parvathi et al. (2012)

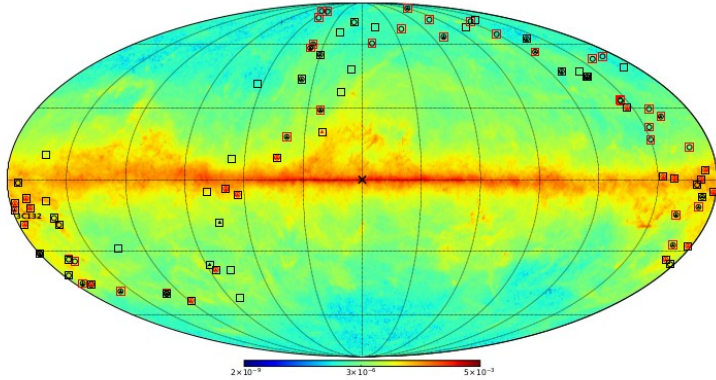
- 21 Galactic sightlines toward neutral medium
CII measurements from the 1334 Å transition
local variations in the total carbon abundance gas+dust
local variations in the carbon depletion



What should a dust model fit for the diffuse ISM ?

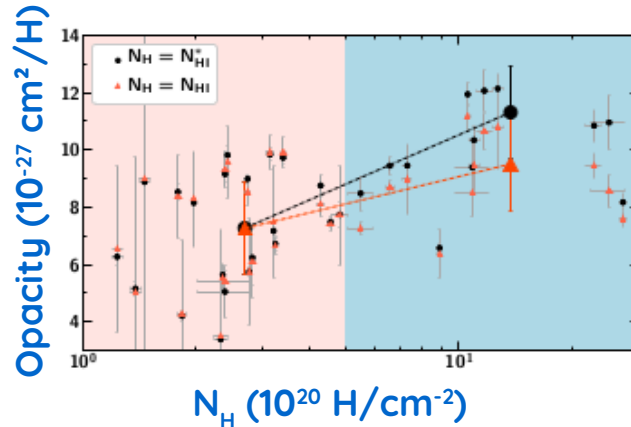
Variations in the dust opacity

Nguyen et al. (2018): 93 LOS with $10^{20} \leq N_H \leq 3 \times 10^{21}$ H/cm²



Optical depth

- 34 atomic lines of sight
+40 % in opacity when $N_H > 5 \times 10^{20}$ H/cm²
- Very little variations in $E(B-V)/N_H$
 $E(B-V) = A_B - A_V$
- Increase in dust mass or change in dust properties ?



Is the canonical Bohlin's ratio still canonical ? No.

Used to normalise dust models

- Bohlin et al. (1978) → $N_{\text{H}}/E(\text{B-V}) = 5.8 \times 10^{21} \text{ cm}^2/\text{mag}$
- Liszt (2014) → $N_{\text{H}}/E(\text{B-V}) = 8.3 \times 10^{21} \text{ cm}^2/\text{mag}$
- Planck Collaboration XI (2014) → $N_{\text{H}}/E(\text{B-V}) = 7 \times 10^{21} \text{ cm}^2/\text{mag}$
- Lenz et al. (2017) → $N_{\text{H}}/E(\text{B-V}) = 8.8 \times 10^{21} \text{ cm}^2/\text{mag}$
- Rémy et al. (2018) → $N_{\text{H}}/E(\text{B-V}) = 3.9 \text{ to } 6.2 \times 10^{21} \text{ cm}^2/\text{mag}$
- Nguyen et al. (2018) → $N_{\text{H}}/E(\text{B-V}) = 9.4 \times 10^{21} \text{ cm}^2/\text{mag}$

Most recent studies find ratios 20 to 60 % higher

Be careful when comparing dust models to what ratio they are normalised

Remember that variations in the dust properties are expected in the diffuse ISM

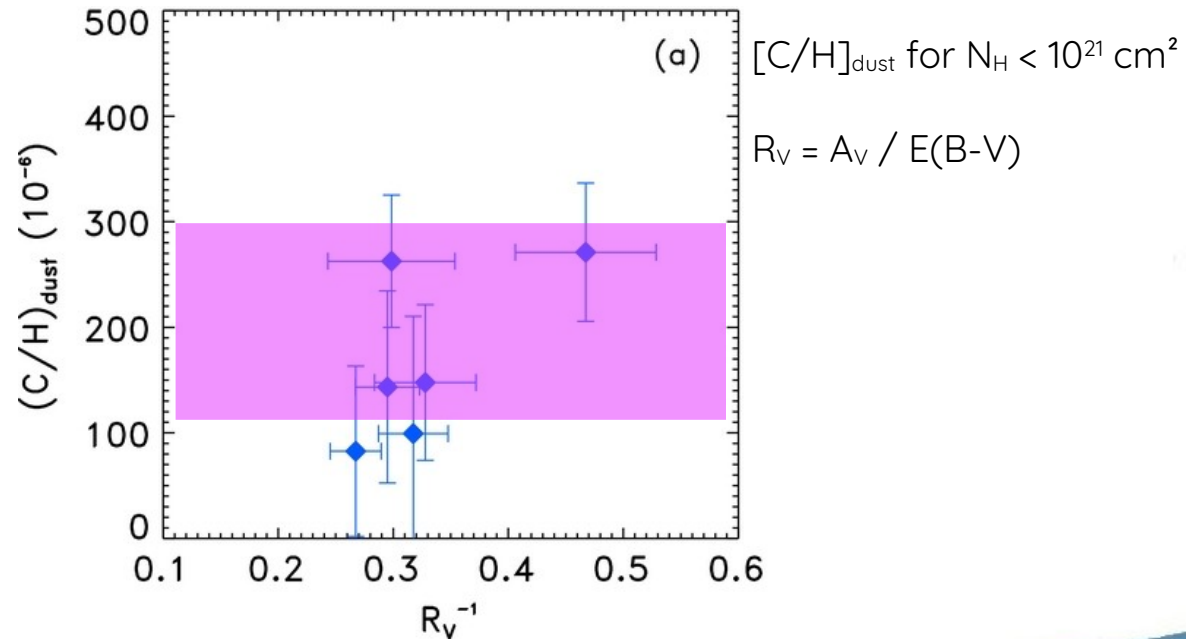
Summary

- **What should a Galactic dust model fit ?**
 - observations of the diffuse ISM
 - **observations of the dense ISM**
 - observations of PDRs
- Dust models: 2 public examples
 - an empirical model
 - a lab-based model
- A few points to bear in mind when using dust models
 - uncertainties in models
 - grain size determination
 - cloud mass estimate

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Carbon depletion in the dense ISM

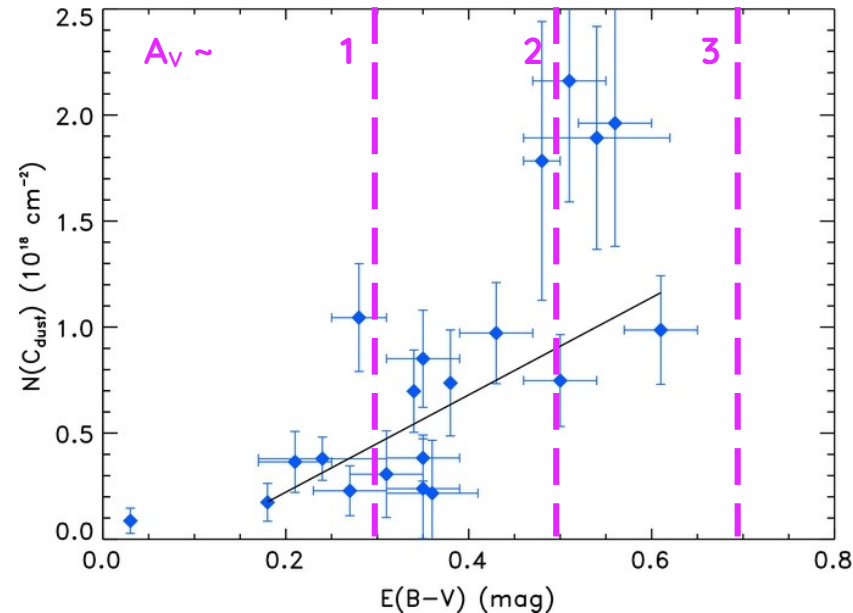
Parvathi et al. (2012)

- What can happen to a grain when the local density increases?

Accretion of gas phase carbon ($A_V > 1-2$) ?

Grain-grain coagulation ($A_V > 2-3$) ?

Ice mantle formation ($A_V > 3$) ?



Column density of C in dust

Carbon depletion in the dense ISM

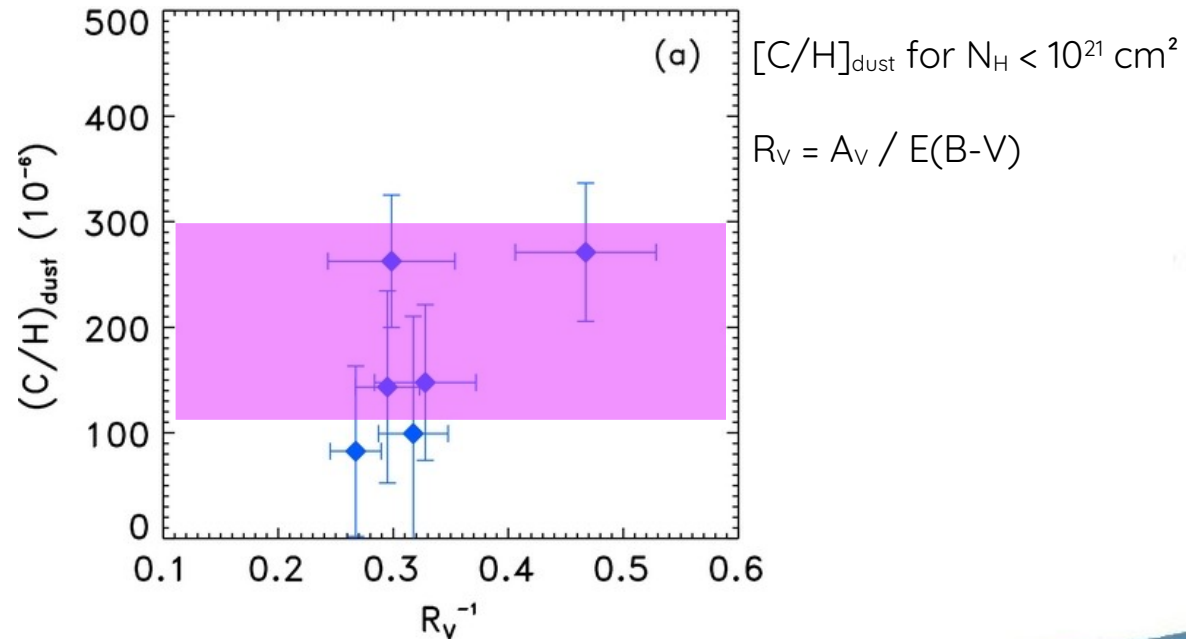
Parvathi et al. (2012)

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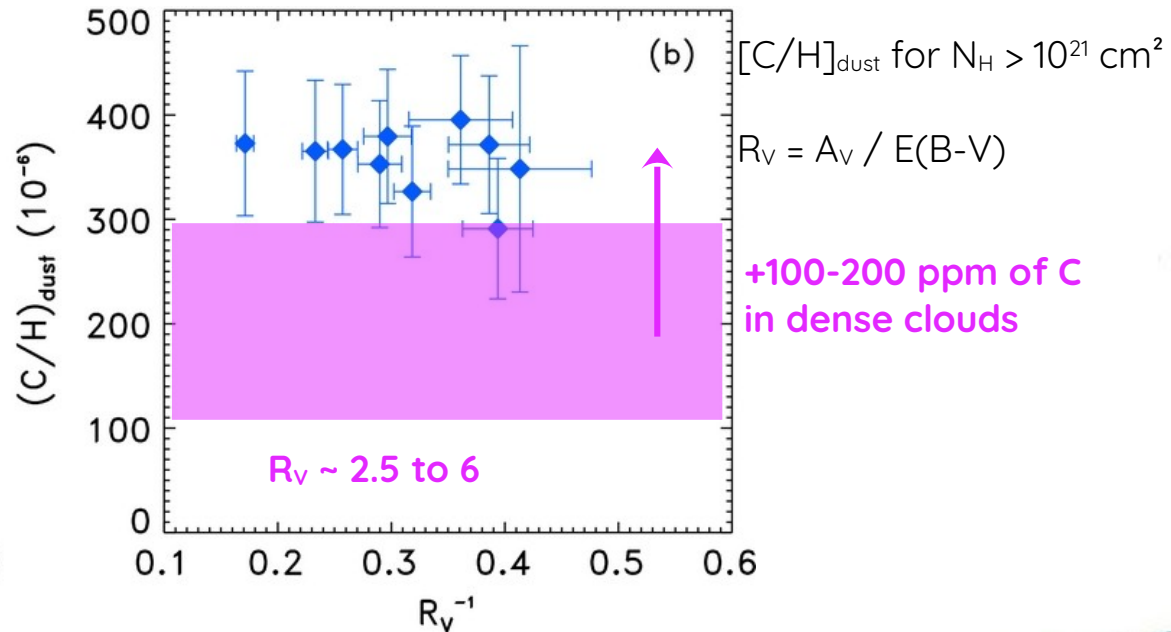
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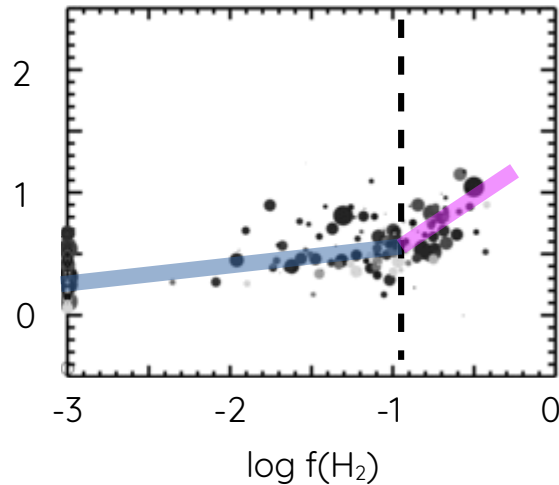
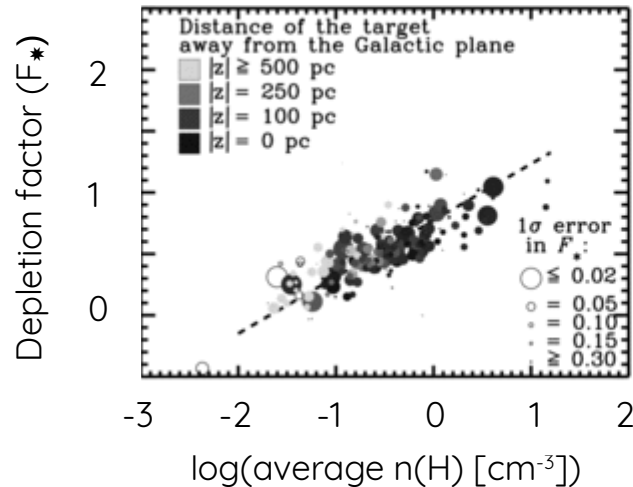
Ice mantle formation ($A_V > 3$) ?



Depletion of heavier elements

Jenkins (2009)

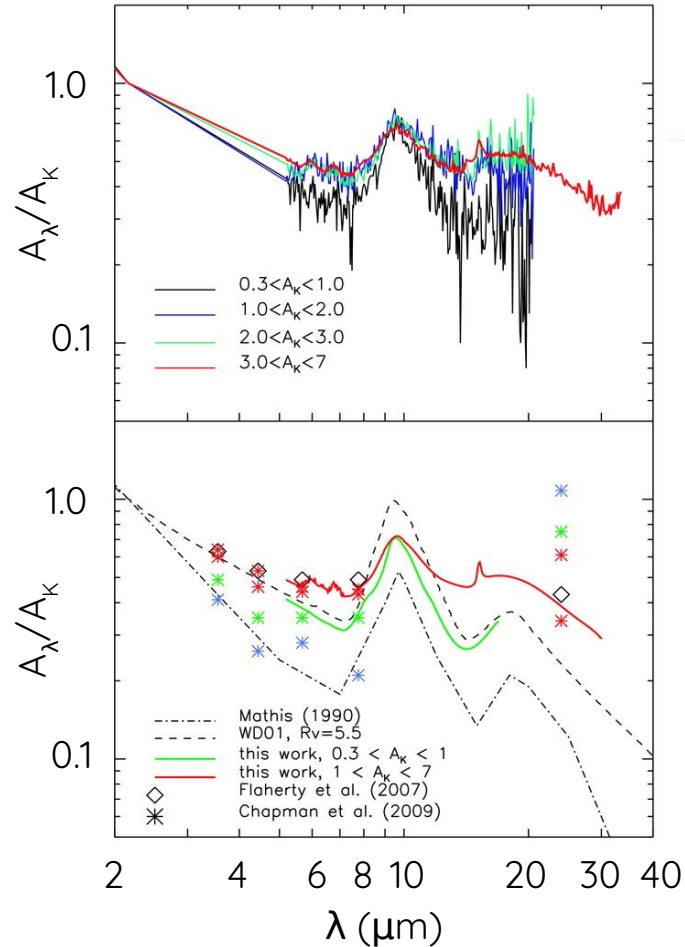
- Depletion of heavier elements
Mg, Si, O, Fe, Cr, Ni, Ti, S...
- Depletion of 17 elements on 243 sightlines
Local variations in $[X_{\text{gas}}/H]$ strengths
Linear relation between the various log. of $[X_{\text{gas}}/H]$



What should a dust model fit for the dense ISM ?

Variations in the silicate mid-IR features

McClure (2009)

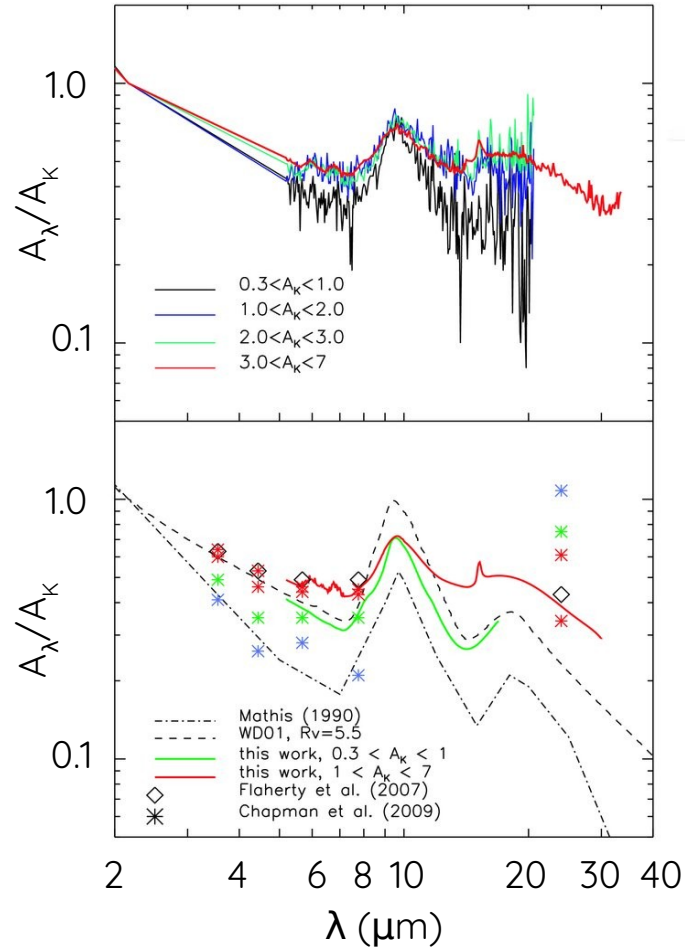


- Sample
 - 24 G0-M4 III stars behind dark clouds
 - Chameleon, Serpens, Taurus
 - Barnard 68, Barnard 59, IC 5146
- Normalisation to K band at 2.2 μm (2MASS)
- Observational results for $A_K > 0.5$ ($\Leftrightarrow A_V \sim 4$)
 - extinction curve flattening
 - widening of both bands
 - BUT peak positions unchanged
 - variations correlated with ice features

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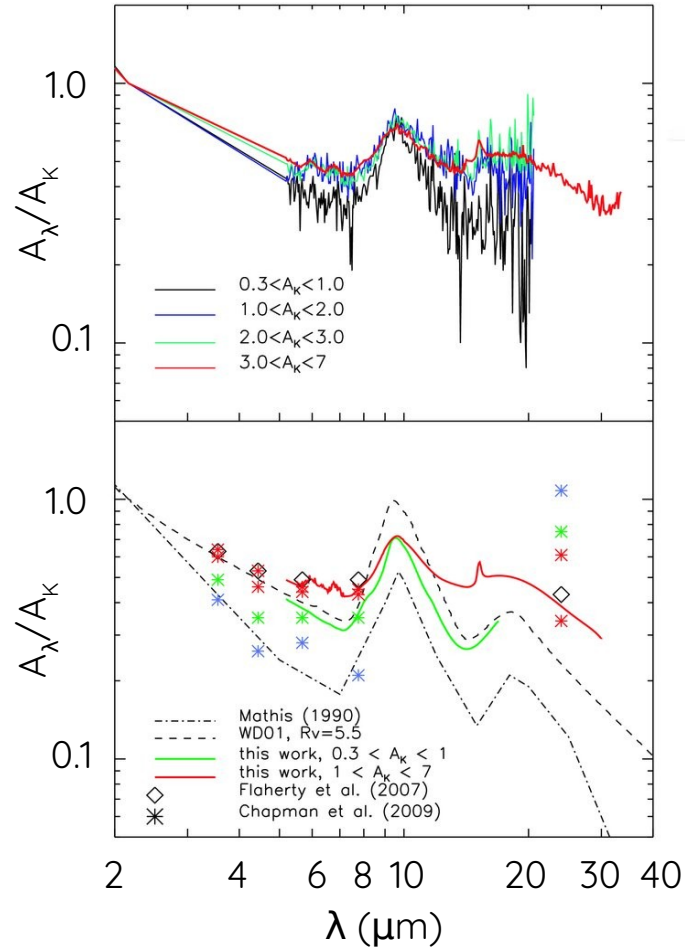
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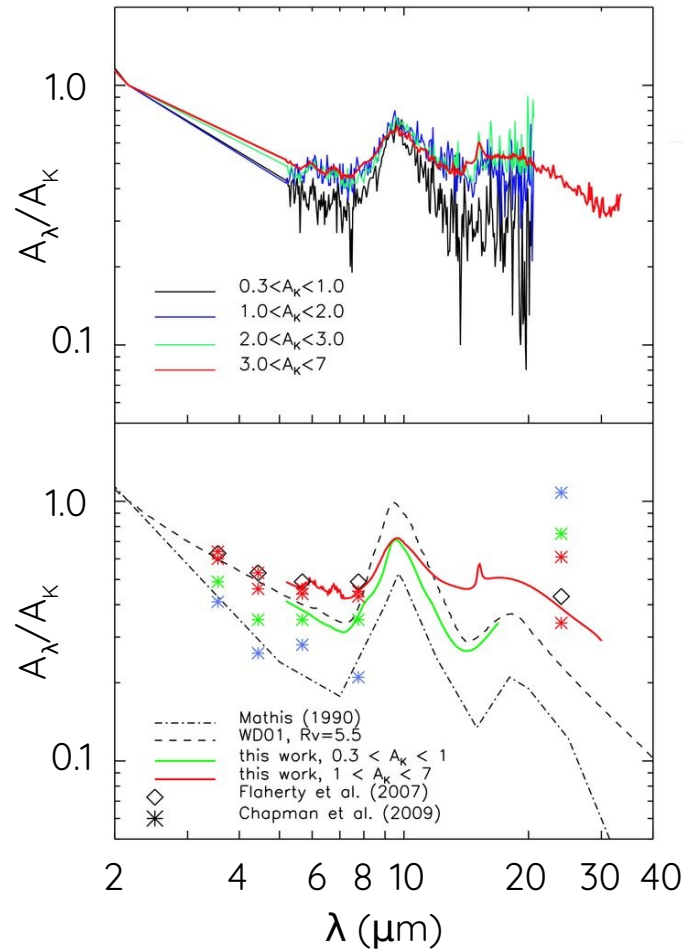
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Carbon accretion ?

What should a dust model fit for the dense ISM ?

Variations in the silicate mid-IR features

McClure (2009)



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extinction curve flattening

widening of both bands

BUT peak positions unchanged

variations correlated with ice features

Grain size cannot exceed $\sim 1 \mu\text{m}$

Carbon accretion ?

Carbon and ice accretion ?

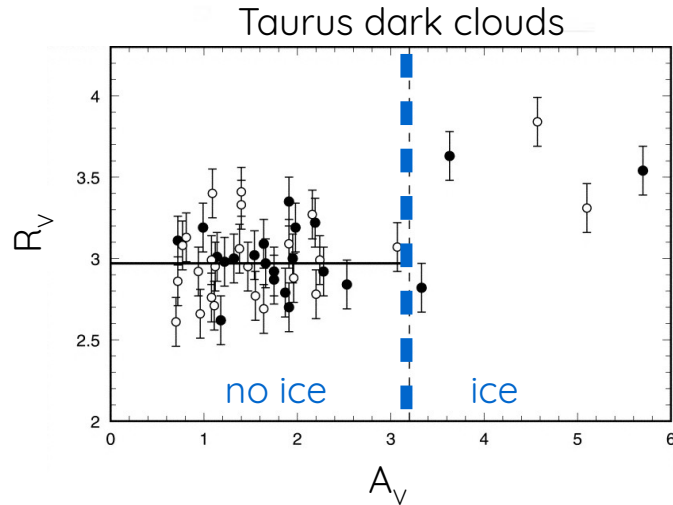
From isolated grains to icy aggregates ?

→ widening only of the $18 \mu\text{m}$ band

What should a dust model fit for the dense ISM ?

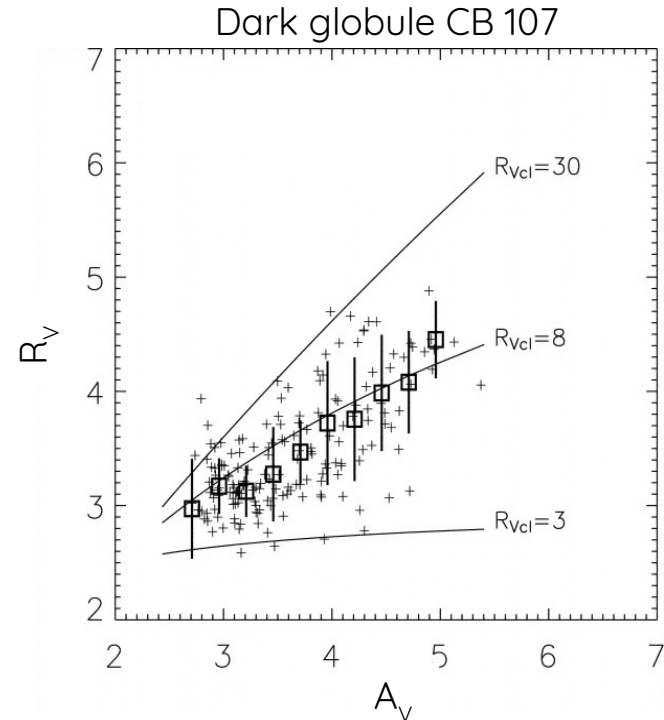
Variations in total-to-selective extinction R_V

Whittet et al. (2001) & Campeggio et al. (2007)



- Increase in R_V with A_V
- Increase when water ice features are detected

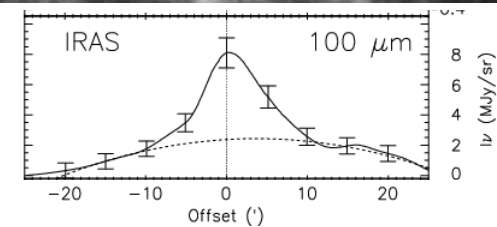
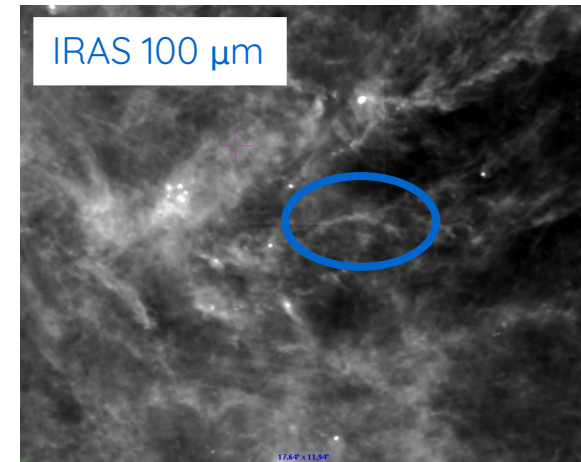
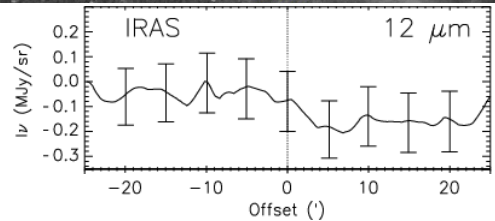
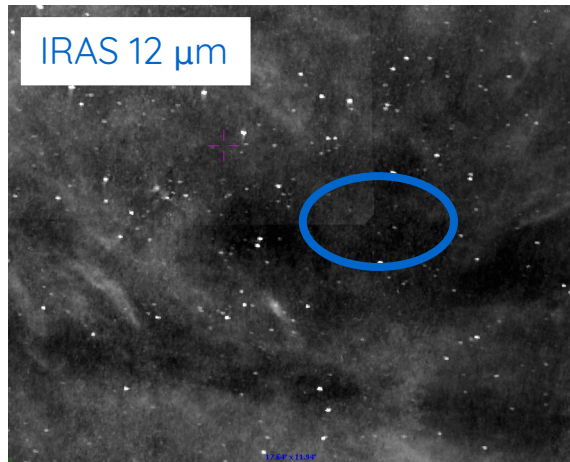
↳ Grain growth associated to ice accretion



What should a dust model fit for the dense ISM ?

Variations in the mid- to far-IR SED

Stepnik et al. (2003)



Not an effect of radiative transfer !

- 🔍 Bernard et al. (1993)
- 🔍 Ysard et al. (2012, 2013)

- No emission in from the mid-IR to $\sim 70 \mu\text{m}$
→ small grains disappear from the diffuse to the dense ISM
- ↳ **Small grain accretion onto larger grains** → **grain growth**

What should a dust model fit for the dense ISM ?

Visible extinction vs. far-IR SED

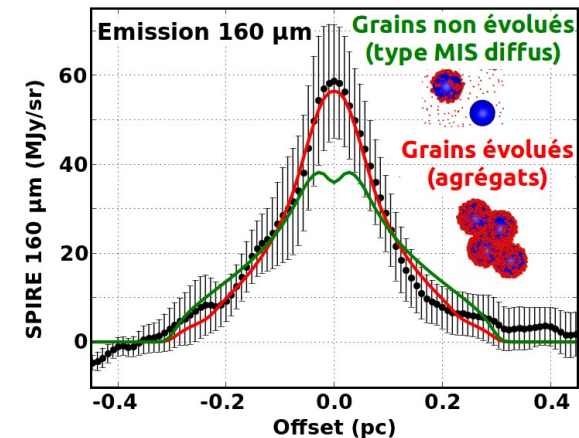
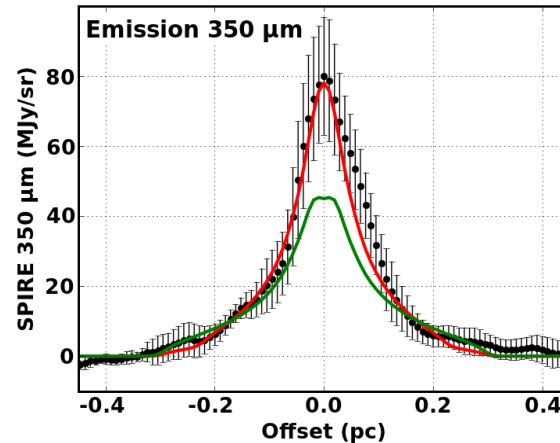
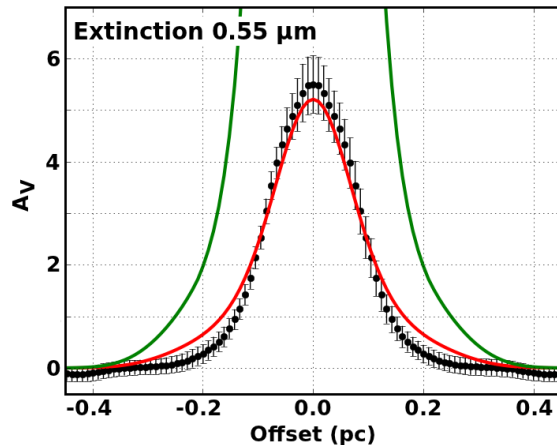
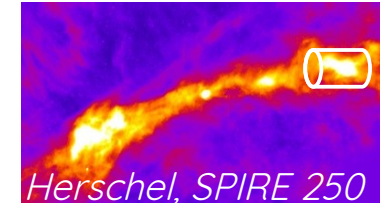
Ysard et al. (2013)

- Aggregates for $1000 < n_{\text{H}} < 2000 \text{ H/cm}^3$
→ $A_V \sim 2$ to 4
- Same as increase in R_V , ice features, mid-IR silicate bands

→ Grain growth

→ From isolated grains to aggregates

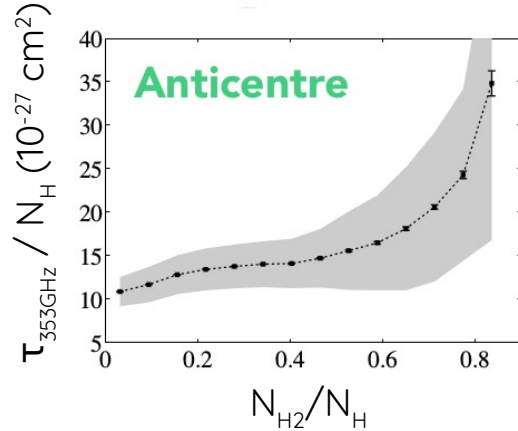
Ysard et al. (2013)



What should a dust model fit for the dense ISM ?

Variations in the far-IR SED

Rémy et al. (2017, 2018)



- Observations of 6 nearby anti-centre clouds
- Usual behaviour of dense clouds

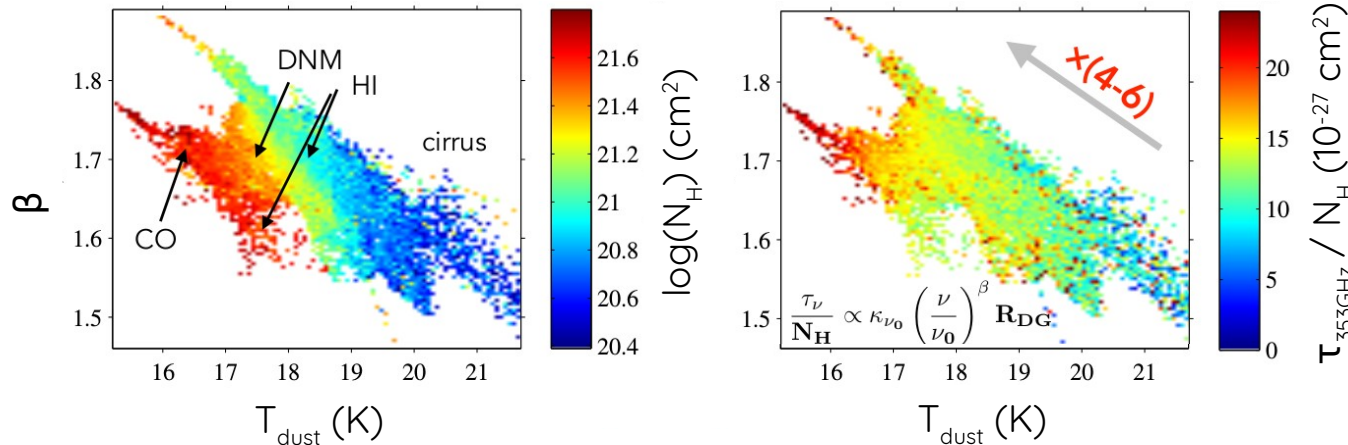
→ T_{dust} ↘
 → $\tau_{\text{submm/FIR}}$ and β ↗

Grain growth

From isolated grains to aggregates
 Carbon accretion ? DCD-TLS ?

🔍 Mény et al. (2007)

🔍 Koehler et al. (2015)

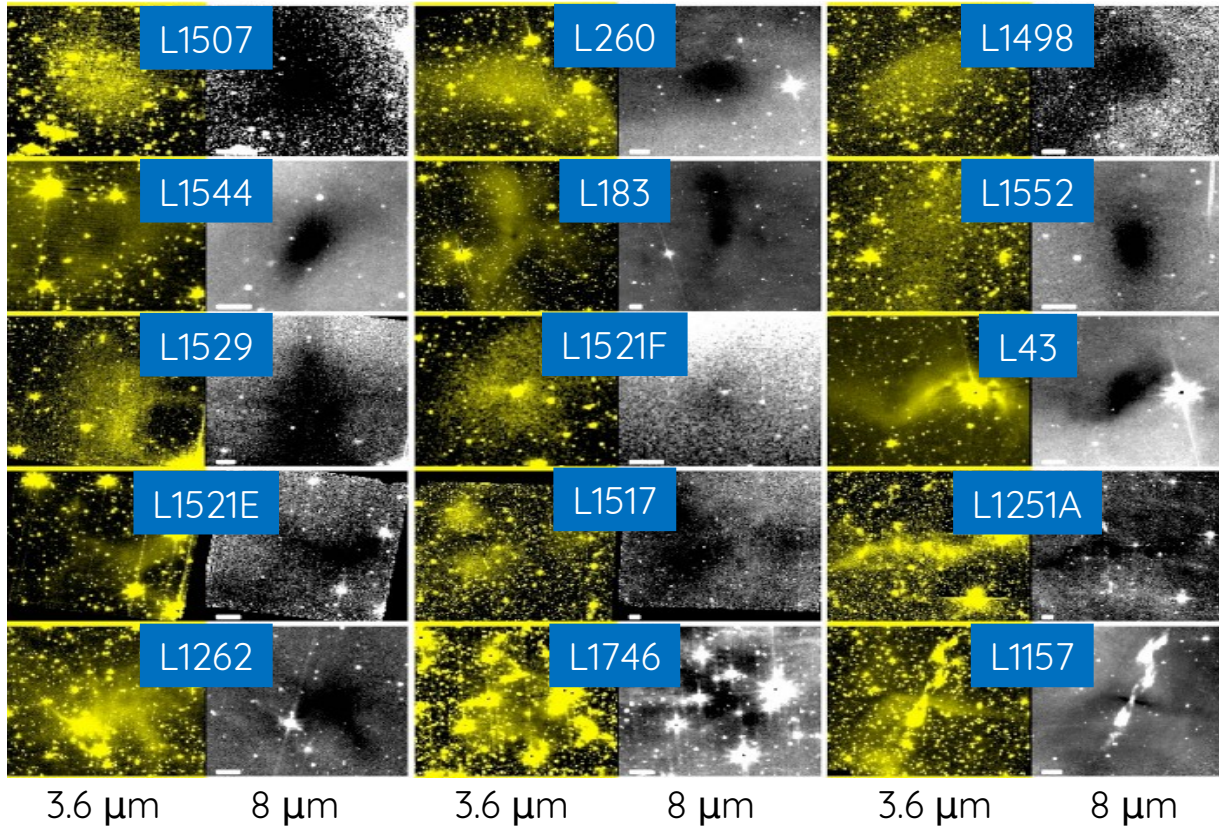


- Gradual evolution across phases significant in DNM stronger in CO

What should a dust model fit for the dense ISM ?

Variations in the dust scattering efficiency

Cloud- & Core-shine



- In the visible: 30's
Struve & Elvey (1936)
- In the near-IR: 90's
Witt et al. (1994)
- In the mid-IR: 2010
Pagani et al. (2010)
- Albedo and asymmetry parameter
Mattila (1970ab, 2018)
- Scattering by bigger grains than in
the diffuse ISM
Steinacker et al. (2010)
Lefèvre et al. (2014)

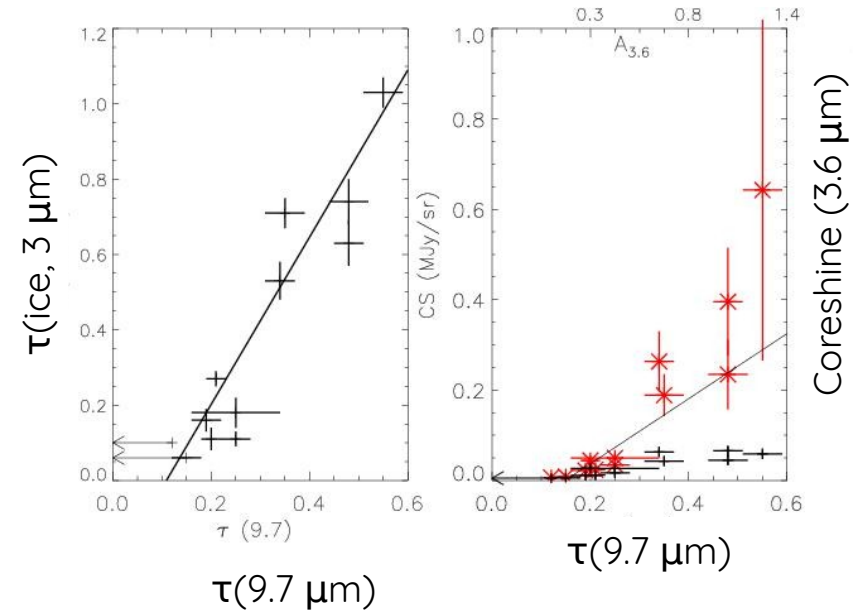
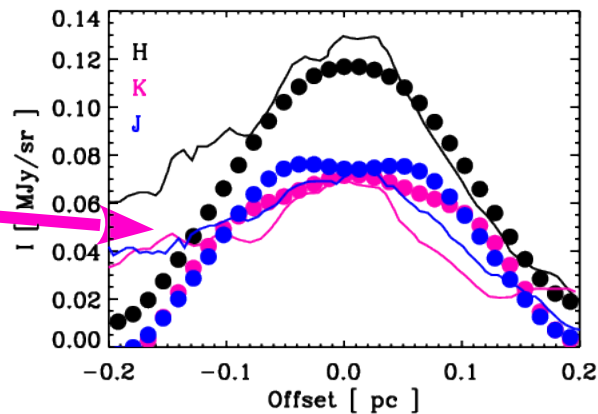
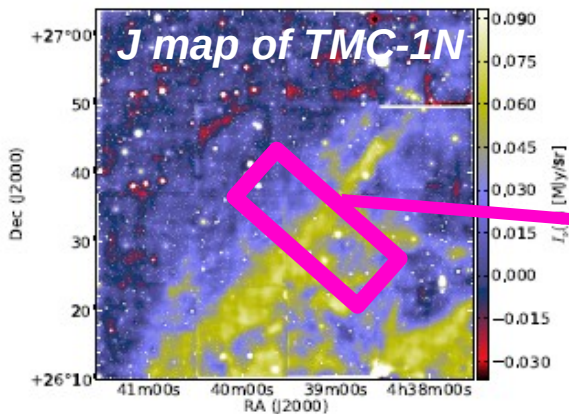
Grain growth

What should a dust model fit for the dense ISM ?

Variations in the dust scattering efficiency

Andersen et al. (2014) & Ysard et al. (2016)

- Andersen et al. (2014)
 - common density threshold for coreshine & ice feature at $3 \mu\text{m}$
- Ysard et al. (2016)
 - need for aggregates when $1000 < n_{\text{H}} < 2000 \text{ H/cm}^3$
 - $A_{\text{V}} \sim 2$ to 4

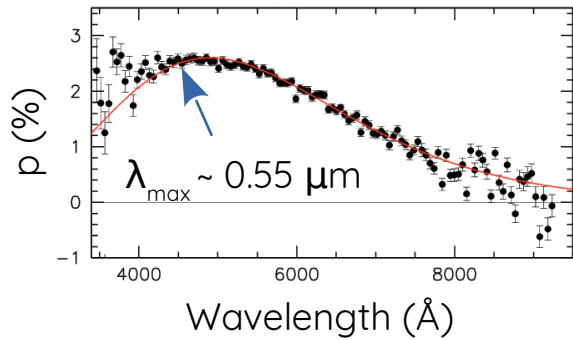


Grain growth
Aggregates?
Ice accretion ?
Carbon accretion ?

What should a dust model fit for the dense ISM ?

Variations in the visible starlight polarisation

Patat et al. (2010): diffuse ISM

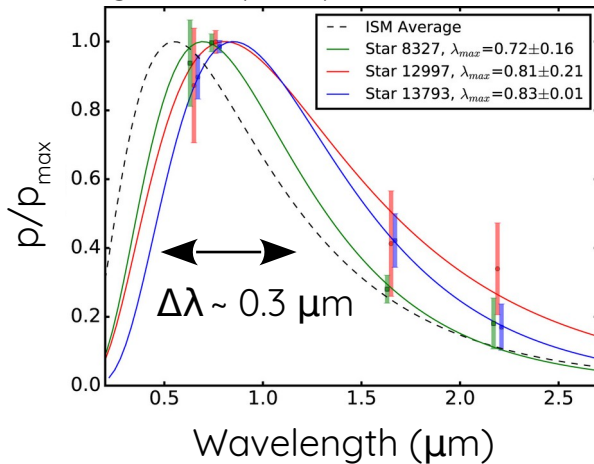


- Linear polarisation of starlight in the visible
→ λ_{max} proportional to aligned $\langle \text{grain size} \rangle$
- Increase in λ_{max} & decrease in $p_{\text{max}}/E(B-V)$ in dense clouds
→ threshold around $A_V = 3-4$

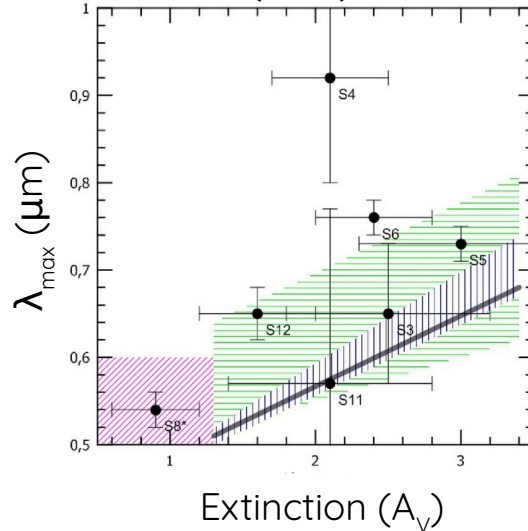
↳ Grain growth

🔍 Fanciullo et al. (2017)

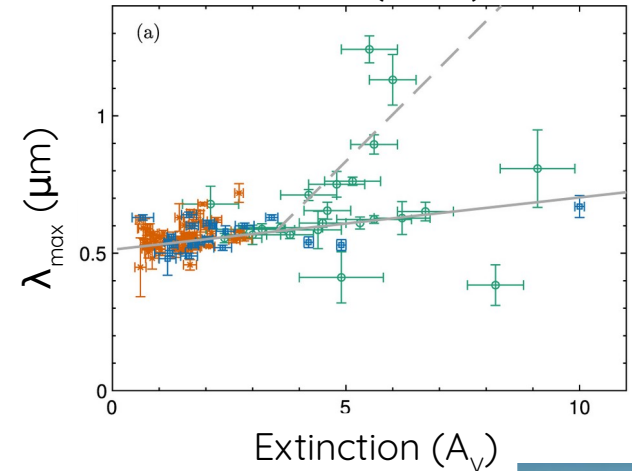
Wang et al. (2017): dark cloud IC5146



Il'in et al. (2018): Barnard 5



Vaillancourt et al. (2020): Taurus MC



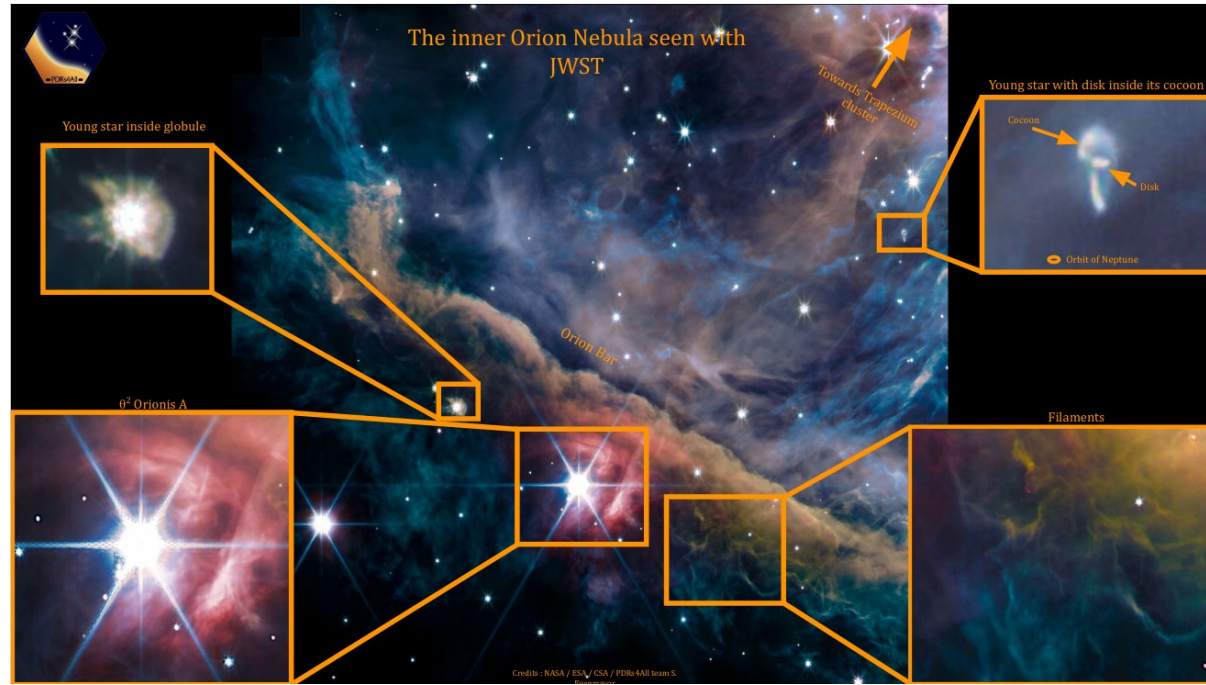
Summary

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What should a dust model fit for PDRs ?

The Orion Bar seen by the JWST (ERS PDR4All)

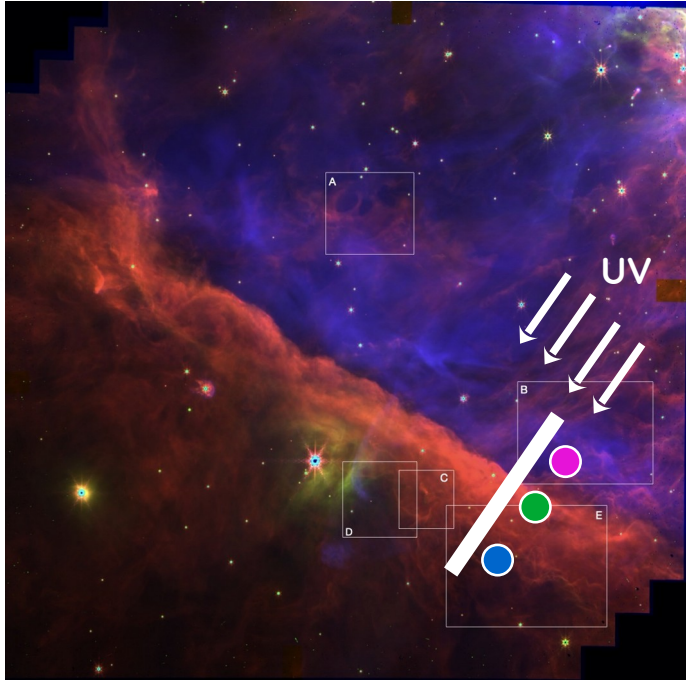
PI: O. Berné, E. Habart, E. Peeters



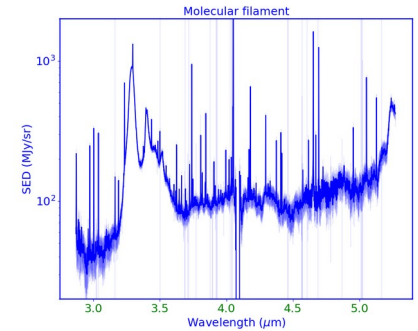
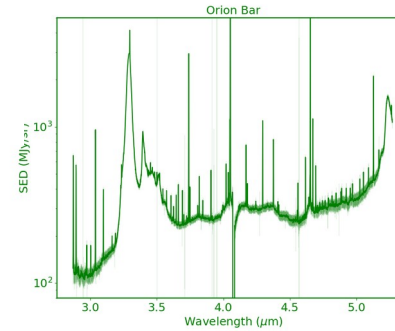
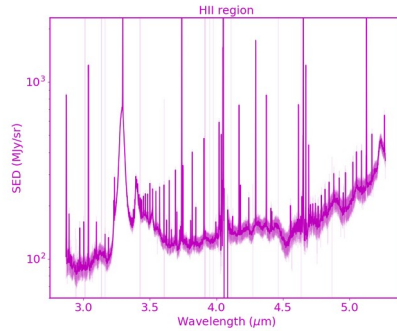
What should a dust model fit for PDRs ?

Dust evolution across the Orion Bar

Elyajouri et al. (in prep)



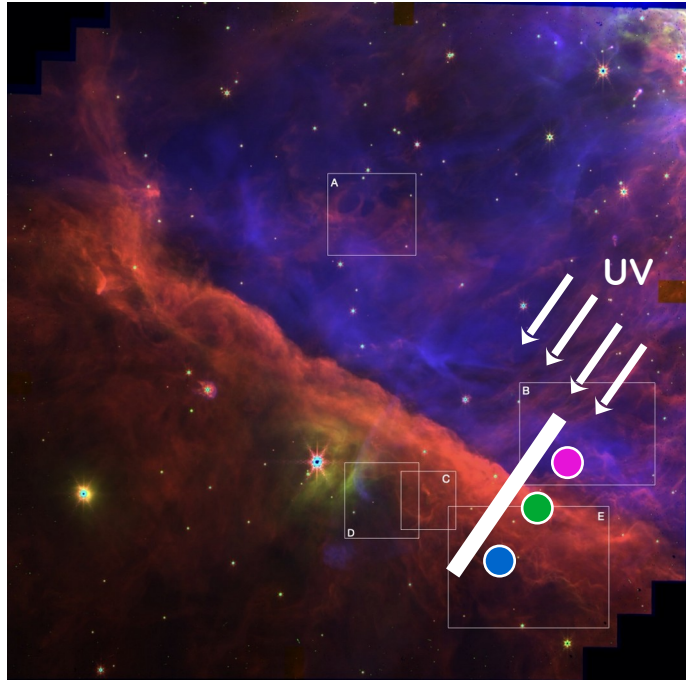
Adapted from Habart et al. (subm.)
Peeters et al. (in prep)



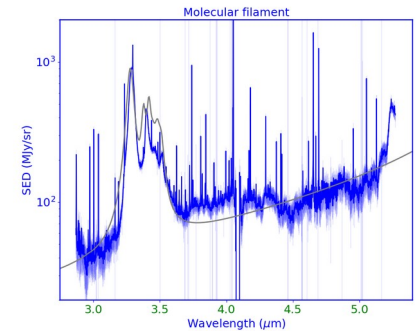
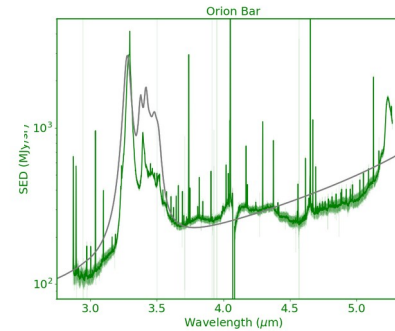
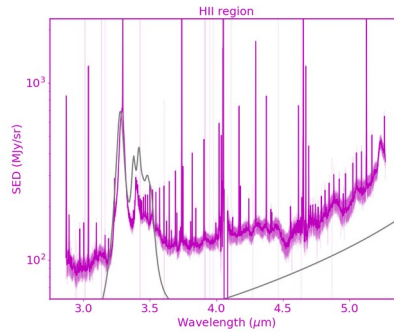
- Variations in band-to-continuum ratio
3.3 to 3.4 band ratio

Dust evolution across the Orion Bar

Nano-grain sizes & hydrogenation



Adapted from Habart et al. (subm.)
Peeters et al. (in prep)



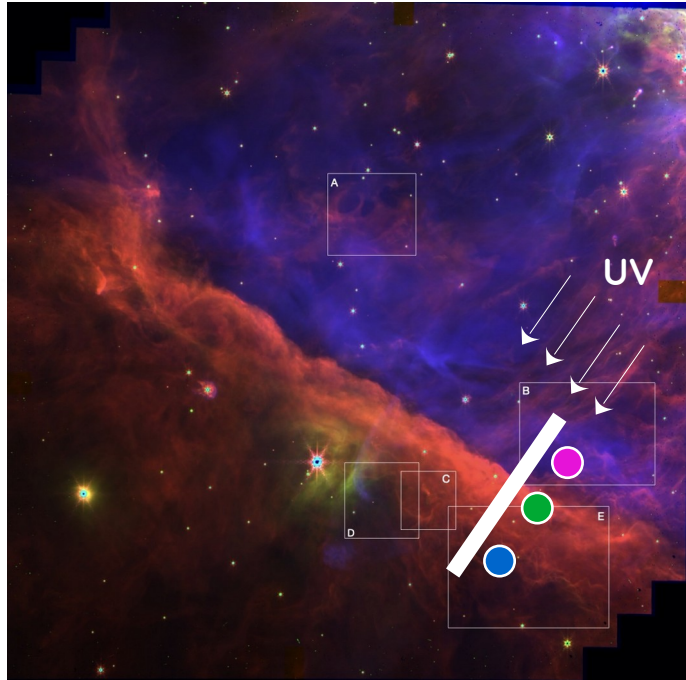
- Variations in band-to-continuum ratio
3.3 to 3.4 band ratio
→ minimum grain size & hydrogenation (E_g)

as in DISM
 $a_{\text{min}} = 0.4 \text{ nm}$
 $E_g = 0.1 \text{ eV} \Leftrightarrow X_{\text{H}} \sim 0.02$

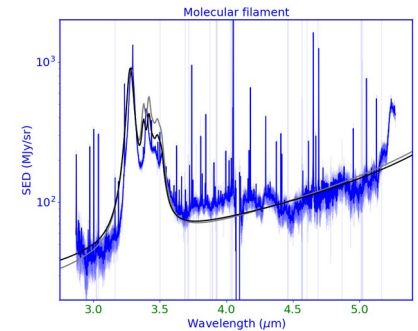
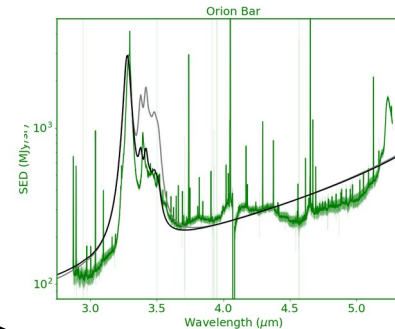
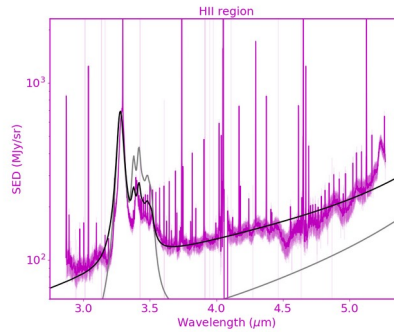
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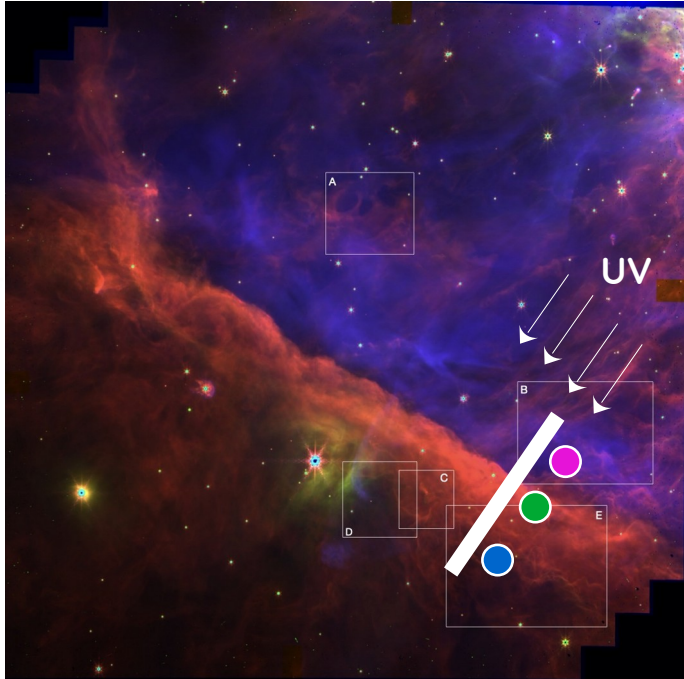
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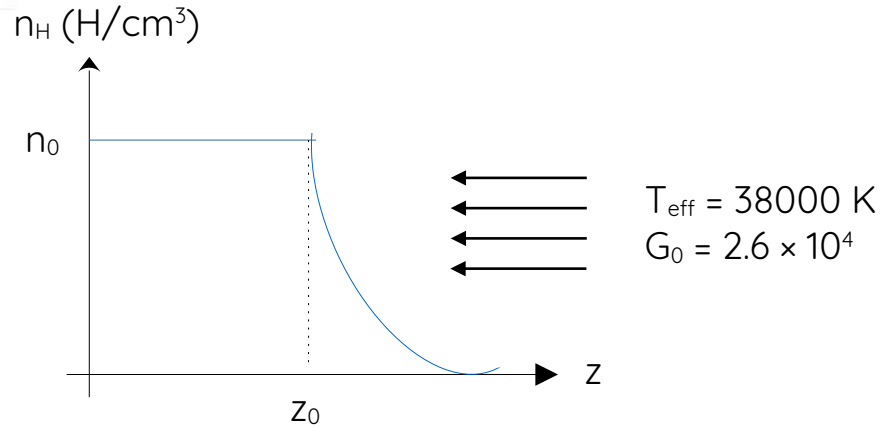
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increasing number of UV photons
decreasing E_g from ~ 0.08 to 0.03 eV
increasing a_{min} from ~ 0.4 to 0.5 nm

Dust evolution across the Orion Bar Radiative transfer model (plane parallel)

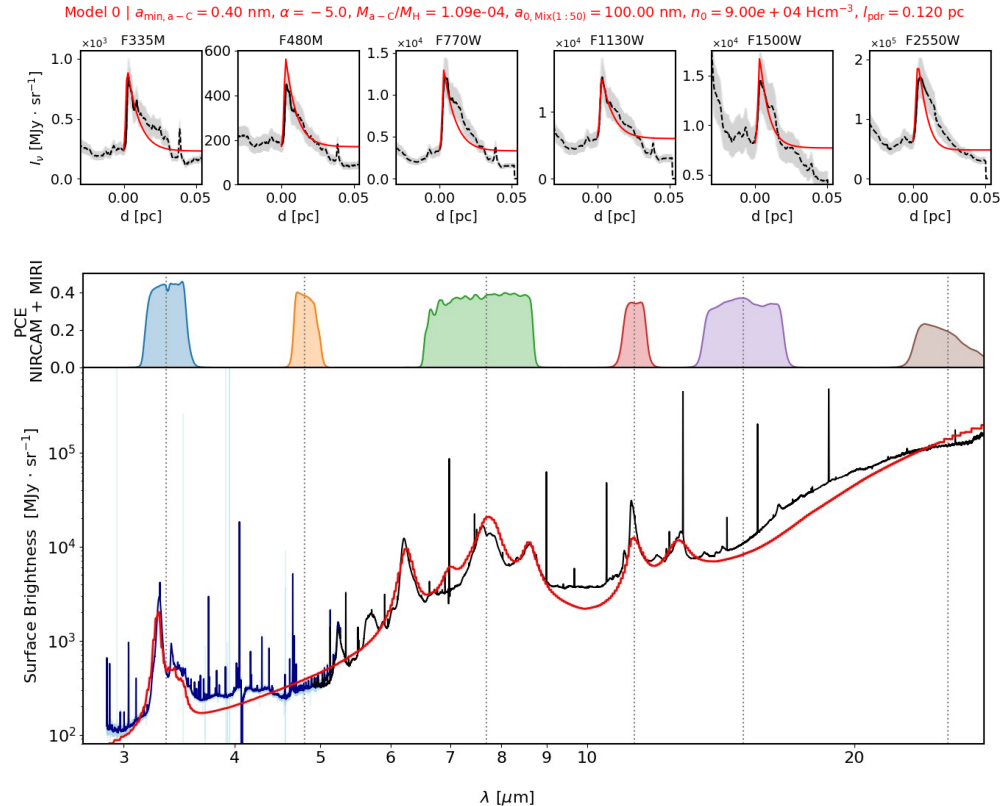


Adapted from Habart et al. (subm.)



same methodology as in Schirmer et al. (2020, 2022)
THEMIS + DustEM + SOC
nano-grains with $E_g = 0.03 \text{ eV}$
pseudo-aggregates from Ysard et al. (2019)

Dust evolution across the Orion Bar



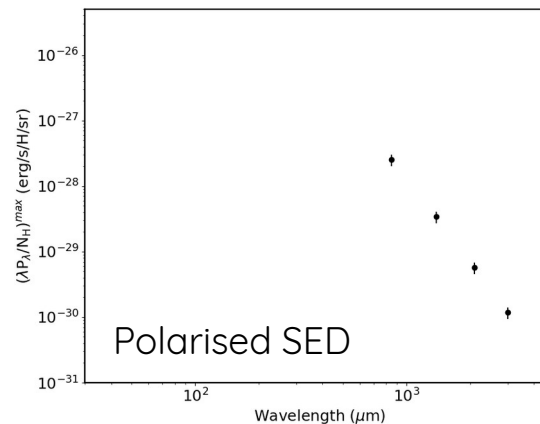
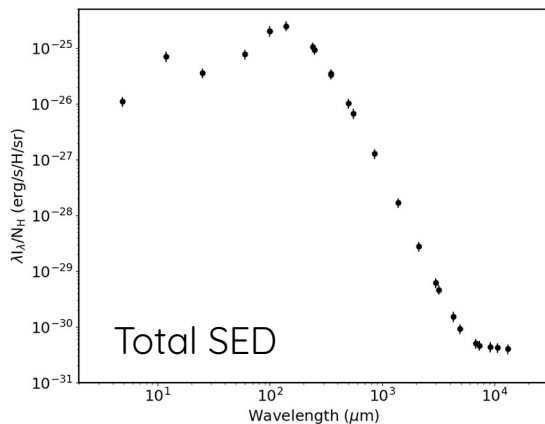
- Fit emission profiles in 6 NIRCam + MIRI filters
A posteriori comparison with NIRSpect and MRS spectra
- 15 times less abundant nano-grains than in the diffuse ISM
- Consequences for estimates of the gas temperature, H₂ formation and intensities of the H₂ pure rotational lines
 - 🔍 Meshaka et al. (in prep.)
 - 🔍 Murga et al. (2023)
 - 🔍 Schirmer et al. (2021)
 - 🔍 Jones & Habart (2015)

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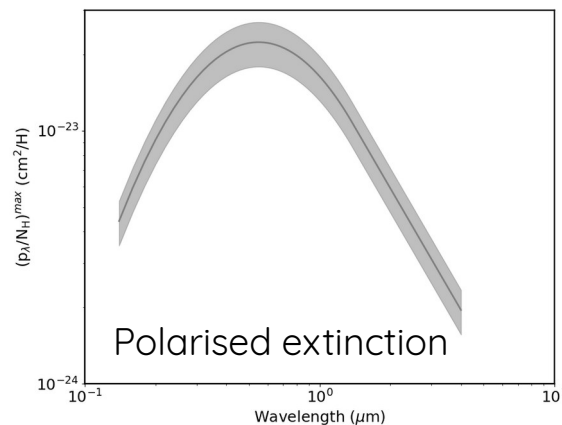
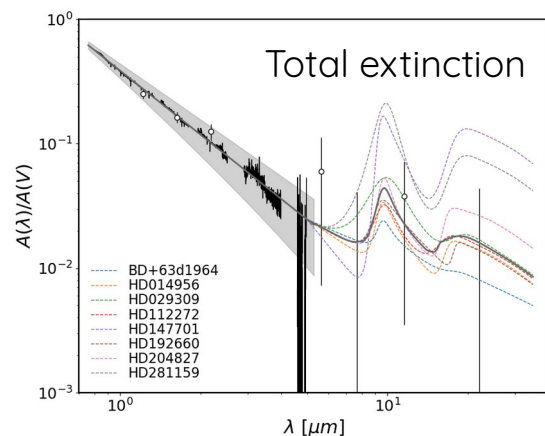
Observational constraints [sky]

Compiègne et al. (2011)
 Planck collab. XVII (2014)
 Planck collab. XXII (2015)
 Bianchi et al. (2017)
 Planck collab. XI (2020)



Planck collab. XXII (2015)
 Planck collab. XI (2020)

Gordon et al. (2021)
 Declair et al. (2022)



Panopoulou et al. (2019)
 Planck collab. XII (2020)

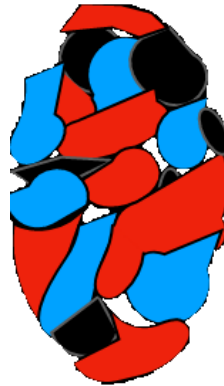
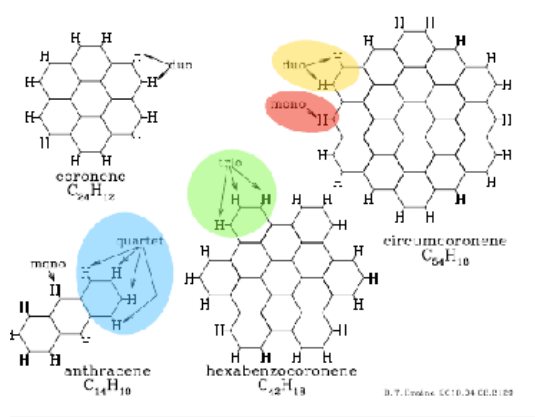
Summary

- What should a Galactic dust model fit ?
 - observations of the diffuse ISM
 - observations of the dense ISM
 - observations of PDRs
- **Dust models: 2 public examples**
 - **an empirical model**
 - a lab-based model
- A few points to bear in mind when using dust models
 - uncertainties in models
 - grain size determination
 - cloud mass estimate

Dust components Draine & Hensley (2021 a)

astroPAHs
Draine & Li (2007)

+ astrodust



Assumption about composition:

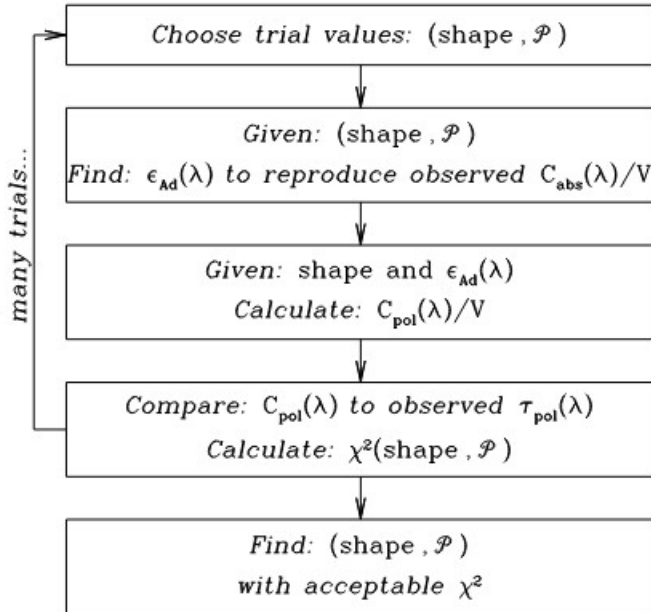
amorphous silicate

hydrocarbon material

other materials (e.g. Fe oxides, Al₂O₃, CaCO₃)

Definition of the astrodust properties

Draine & Hensley (2021 a, b, c)



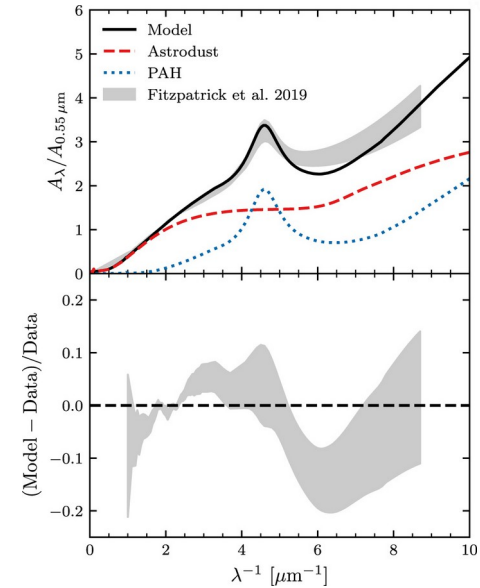
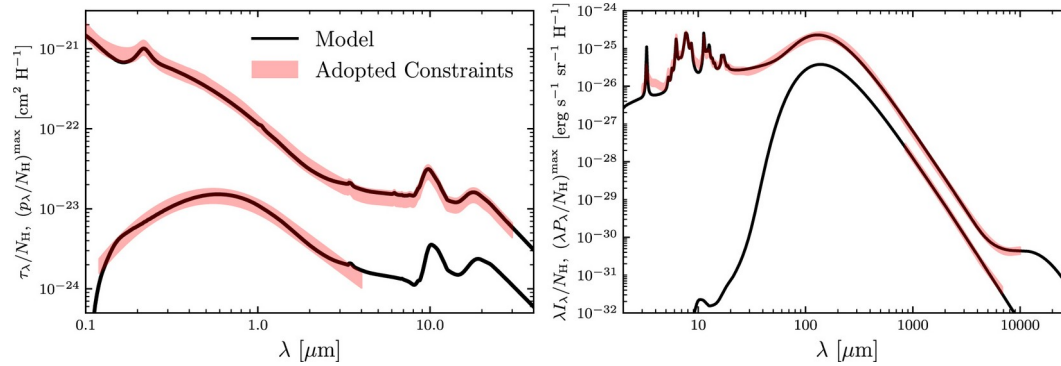
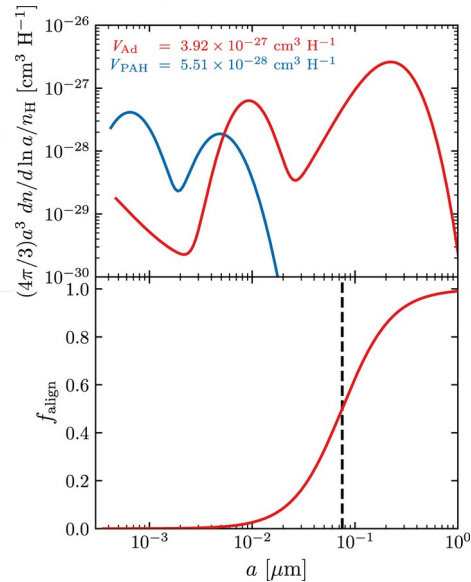
- Use of IR absorption to empirically derive a complex dielectric function for “astrodust” that fits perfectly the observations (in the Rayleigh limit, $a \ll \lambda$, extinction dominated by absorption and C_{abs}/V is directly related to ϵ_{ad} and independent of a)

$$\langle \kappa_{abs} \rangle = \frac{2\pi N}{3\rho\lambda} \text{Im} \left(\frac{\epsilon - \epsilon_m}{\epsilon_m + L(\epsilon - \epsilon_m)} + \frac{4(\epsilon - \epsilon_m)}{2\epsilon_m + (1 - L)(\epsilon - \epsilon_m)} \right)$$

- Check if consistent with polarised extinction
➔ Gets optical properties associated with shape and porosity

Figure 1. Approach used to determine the shape and dielectric function ϵ_{Ad} of the silicate-bearing “astrodust” grains. \mathcal{P} is the porosity of the astrodust grains (see text).

Fitting results Hensley & Draine (2022)



- 🔍 Draine & Hensley (2021 a, b, c)
- 🔍 Hensley & Draine (2020, 2022)
- 🔍 Draine (2016)
- 🔍 Draine & Li (2007)

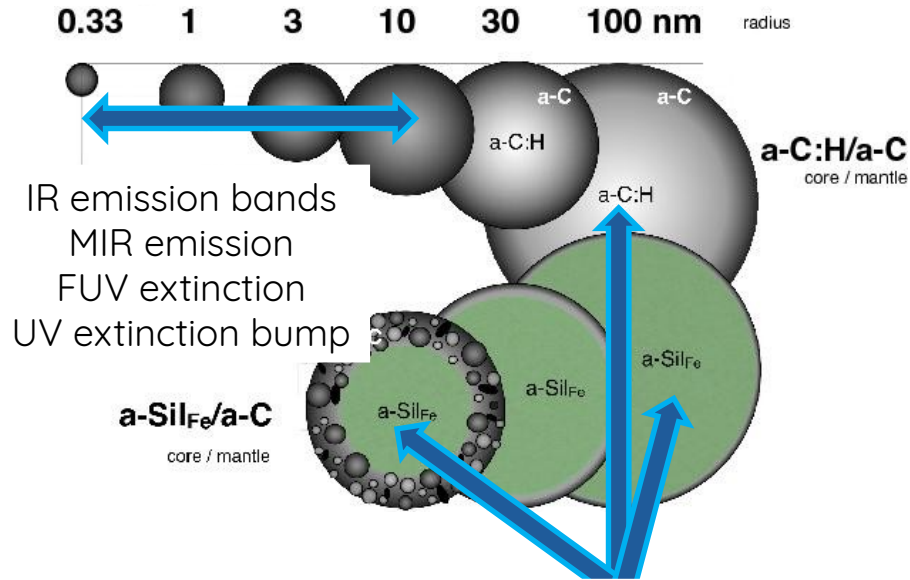
Dust model available here:
<https://dataverse.harvard.edu/dataverse/astrodust>

Summary

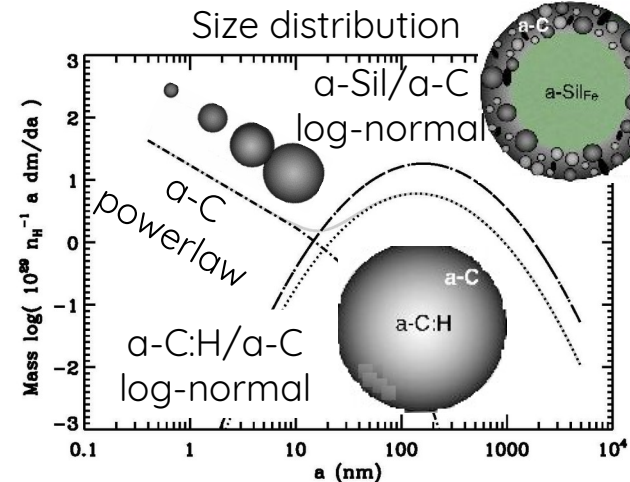
- What should a Galactic dust model fit ?
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Dust components

Jones et al. (2013)



IR absorption bands
visible/MIR extinction
FIR/submm emission



- 🔍 Jones, Köhler, Ysard et al. (2017)
- 🔍 Ysard, Köhler, Jones et al. (2015)
- 🔍 Köhler, Jones & Ysard (2014)
- 🔍 Jones et al. (2013)

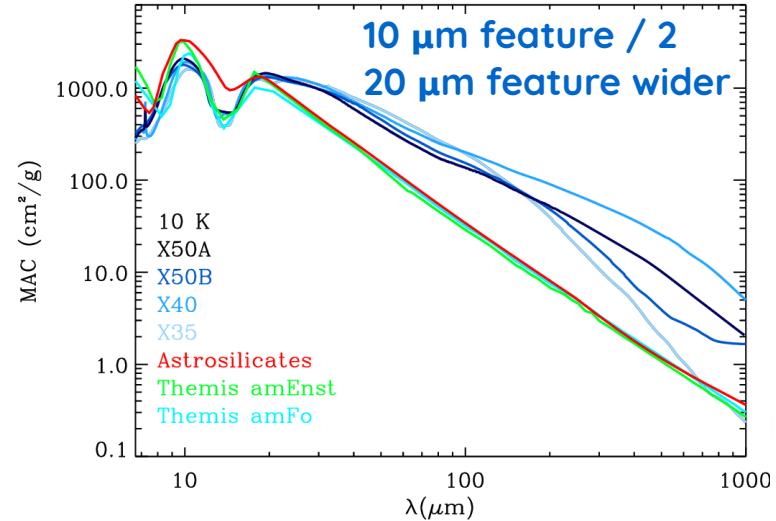
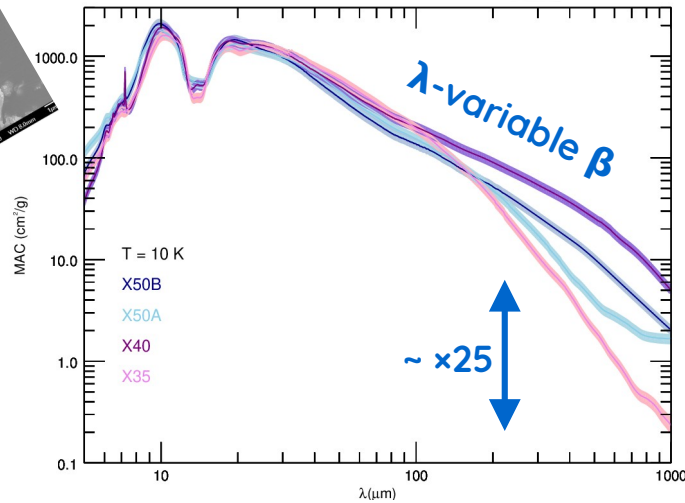
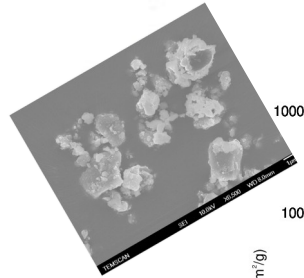
Dust model available here:

<https://www.ias.u-psud.fr/themis/>

<https://www.ias.u-psud.fr/DUSTEM/>

Observational constraints [lab]

Demyk et al. (2017, 2022)

Mass absorption coefficients of amorphous Mg-rich silicates from 5 μm to 1 mm

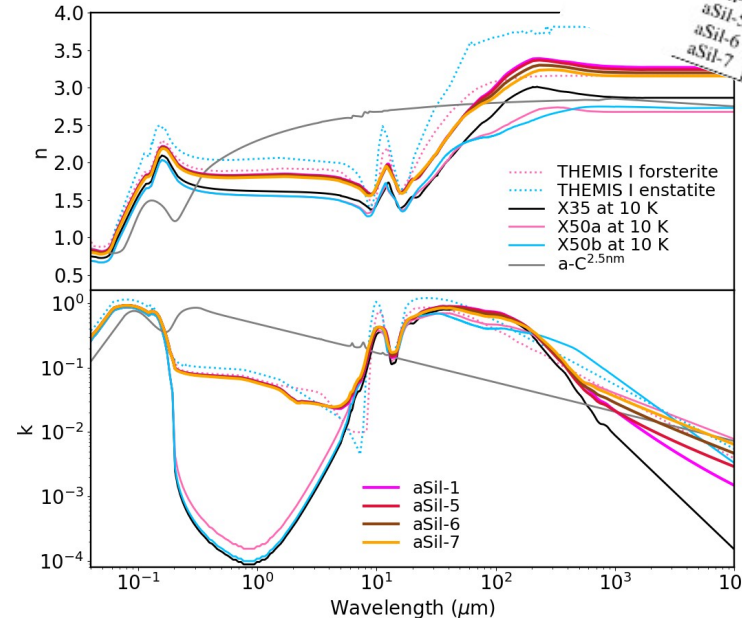
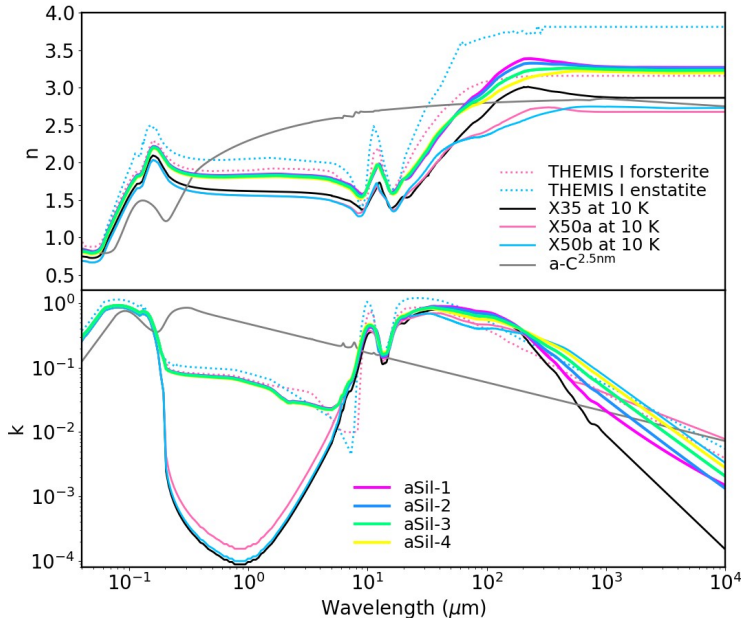
- X35 \rightarrow stoichiometry of forsterite
X50a, X50b \rightarrow stoichiometry of enstatite
X40 \rightarrow in-between
- Major differences at all wavelengths, high variability with wavelength and composition

Optical constants → silicate grains

Ysard et al. (to be subm.)

Table 1. Silicate core compositions with corresponding line colours in the figures.

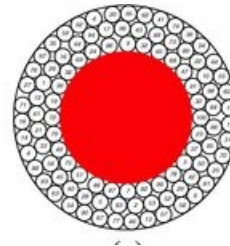
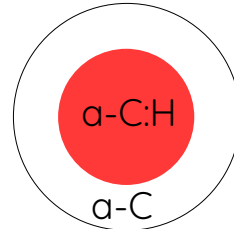
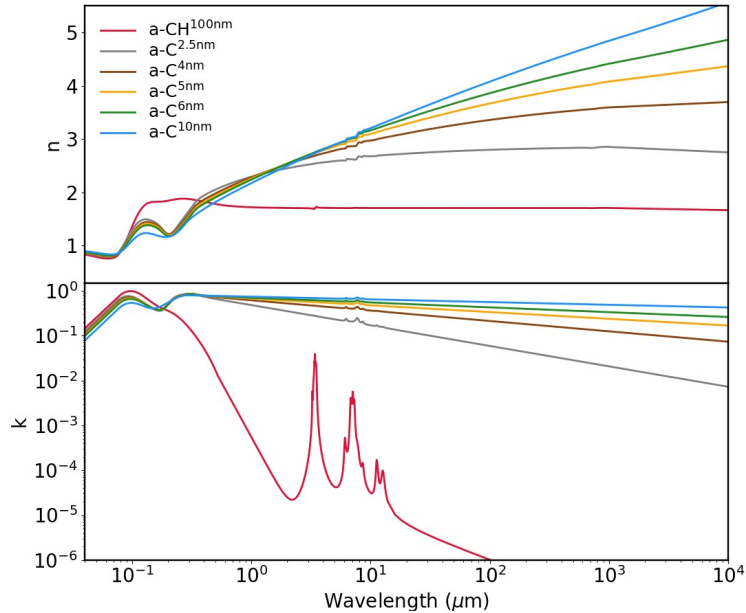
| Name | X35 | X50a | X50b | Colour |
|--------|-----|------|------|---------|
| aSil-1 | 80% | 10% | 10% | magenta |
| aSil-2 | 70% | - | 30% | blue |
| aSil-3 | 50% | - | 50% | green |
| aSil-4 | 30% | - | 70% | yellow |
| aSil-5 | 70% | 30% | - | red |
| aSil-6 | 50% | 50% | - | brown |
| aSil-7 | 30% | 70% | - | orange |



- Spectral index variations from 2.5-3.0 to 1.7-2.5 from far-IR to mm
- Submm absorption efficiencies $\times 1.5$
- Mid-IR silicate features shift by a few $0.1 \mu\text{m}$

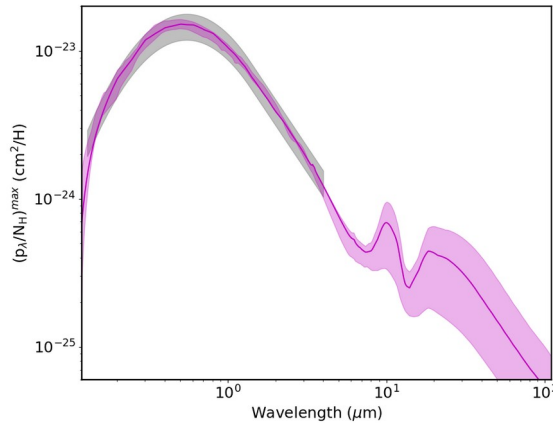
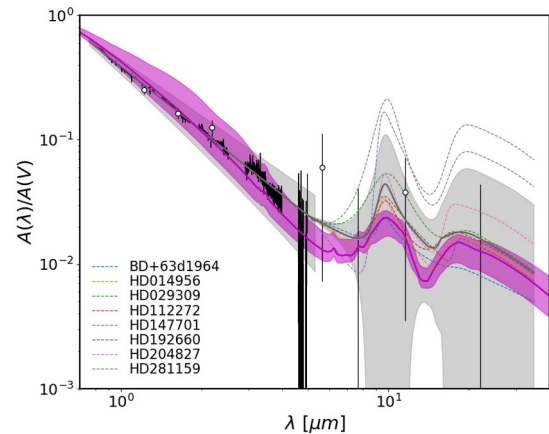
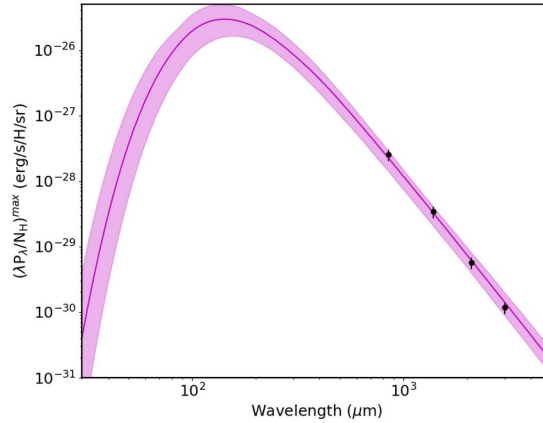
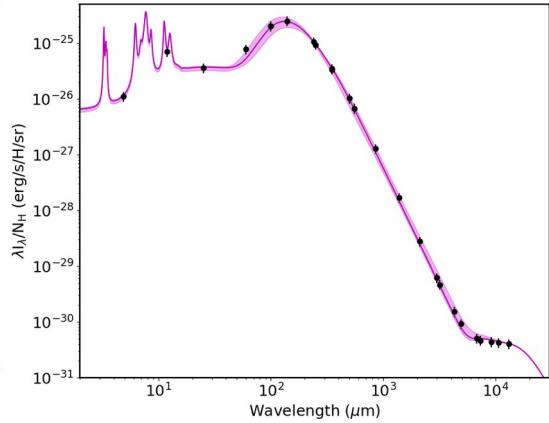
Optical constants → carbonaceous grains

Description of the mantle

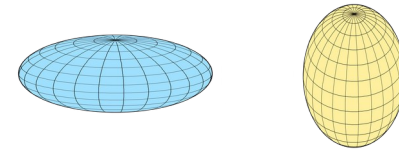


- From a-C:H/a-C^{2.5nm} to a-C:H/a-C^{10nm}
 - far-IR/submm $Q_{\text{abs}} \times 4$
 - $\beta = 1.35$ to 1.12
 - T decrease by ~ 5 K

Fitting results



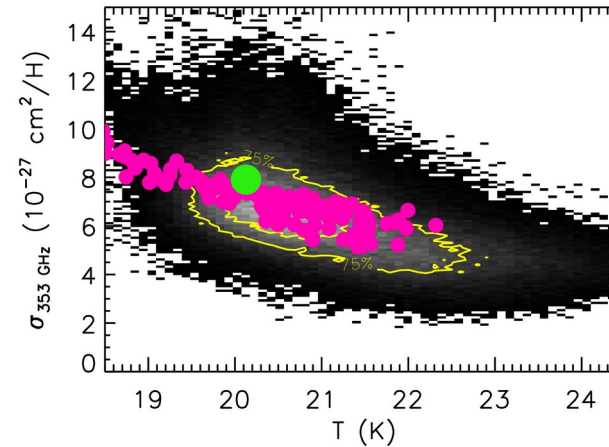
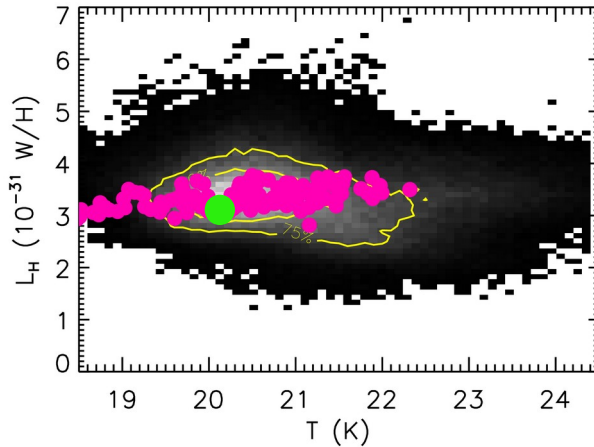
- Core/mantle spheroidal grains with $e = 1.3$ & 2
 - oblates
 - prolates



- All shapes yield acceptable solutions
- All silicate compositions too
- $0.9 \leq G_0 \leq 1.2$

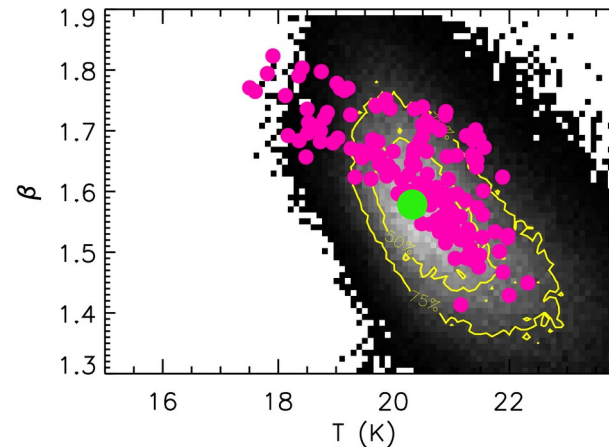
↳ No unique solution

Comparison with Planck collaboration XI (2014)



- astro dust + astroPAHs
- various lab silicates + α -C

Laboratory data in agreement with:
 → average high latitude SED & extinction
 → dispersion in the derived dust parameters

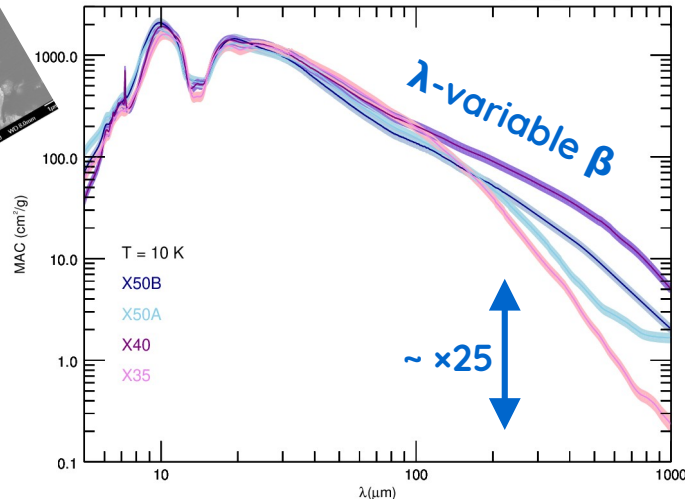
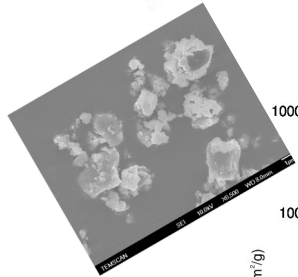


Summary

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Uncertainties in the optical constants

Demyk et al. (2017, 2022)



Uncertainties on size distribution
 shape distribution
 visible optical properties

$\Delta n < 10 \%$
 $5 \% < \Delta k < 20 \%$

$$\epsilon = m^2$$

$$n = \sqrt{\frac{\sqrt{\epsilon'^2 + \epsilon''^2} + \epsilon'}{2}}$$

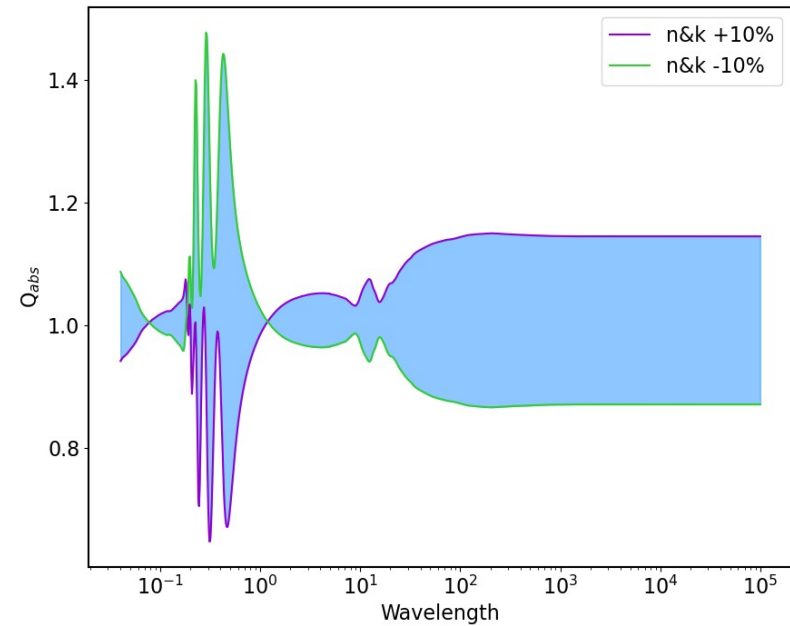
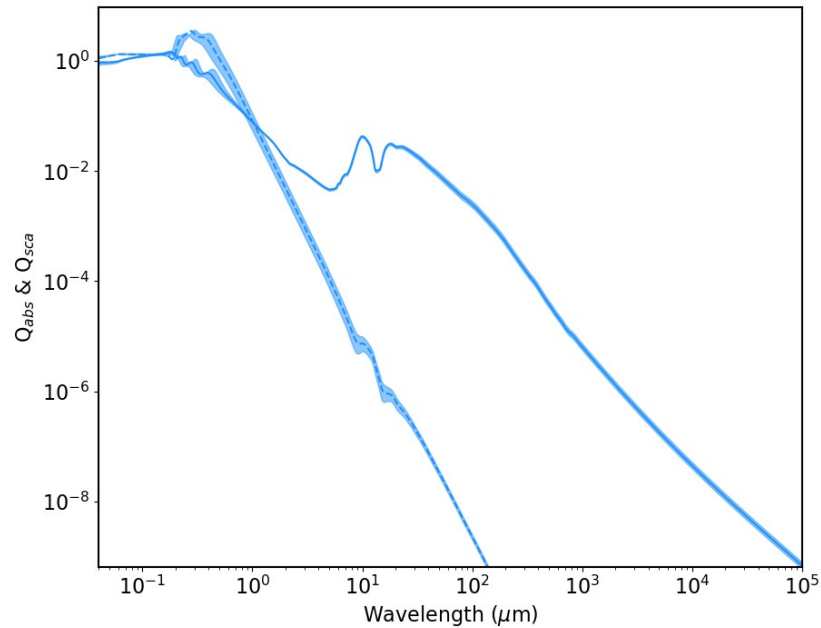
$$k = \sqrt{\frac{\sqrt{\epsilon'^2 + \epsilon''^2} - \epsilon'}{2}}$$

$$\langle \kappa_{\text{abs}} \rangle = \frac{2\pi N}{3\rho\lambda} \text{Im} \left(\frac{\epsilon - \epsilon_m}{\epsilon_m + L(\epsilon - \epsilon_m)} + \frac{4(\epsilon - \epsilon_m)}{2\epsilon_m + (1 - L)(\epsilon - \epsilon_m)} \right)$$

Uncertainties in the optical constants

→ translation in the Q_{abs} & Q_{sca}

Let's assume that both n & k vary by +10 % or -10 % for silicates
 $a = 0.1 \mu\text{m}$

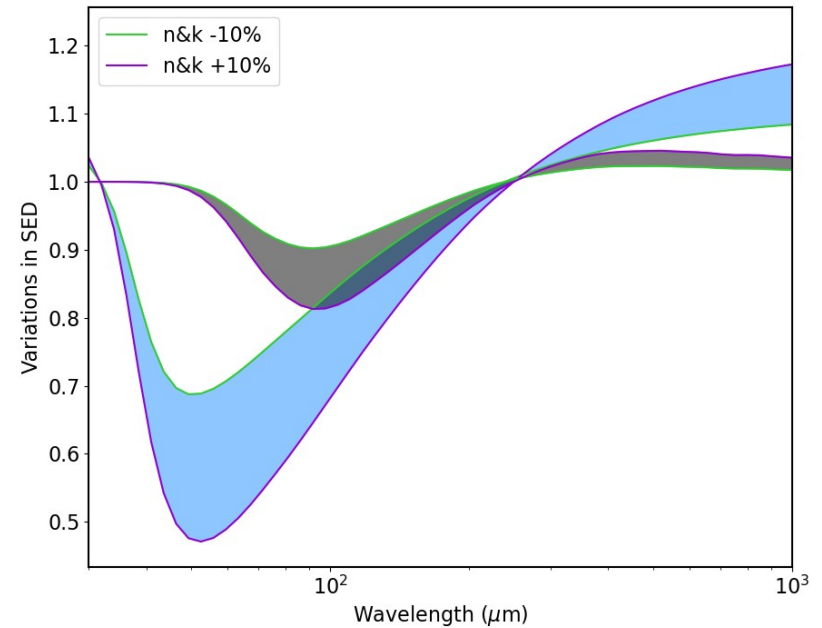
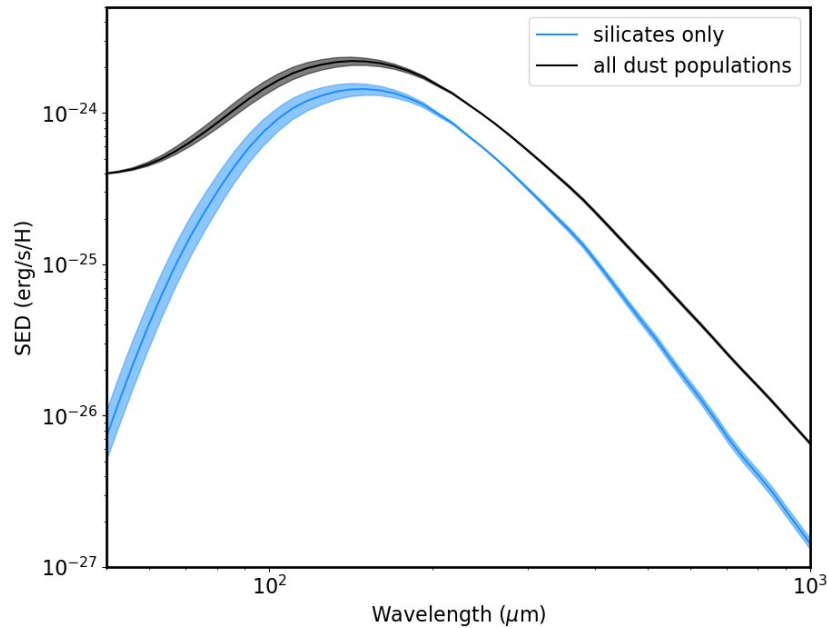


Uncertainties in the optical constants

→ translation in the SED

Let's assume that both n & k vary by +10 % or -10 % for silicates

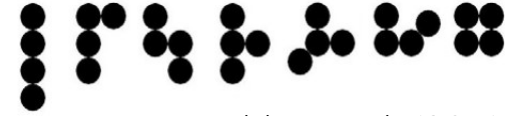
→ silicates with a log-normal size distribution



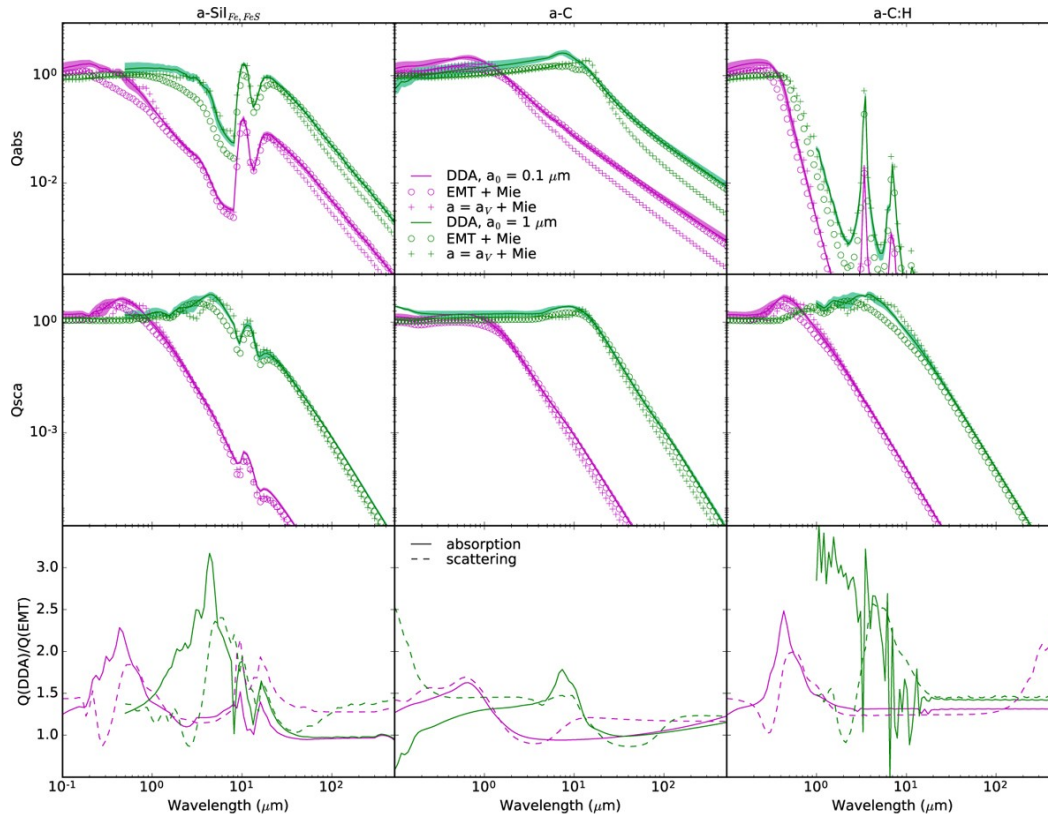
→ 10 % at long wavelength

→ more around the peak of the SED due to \neq temperatures

Choice of the calculation method



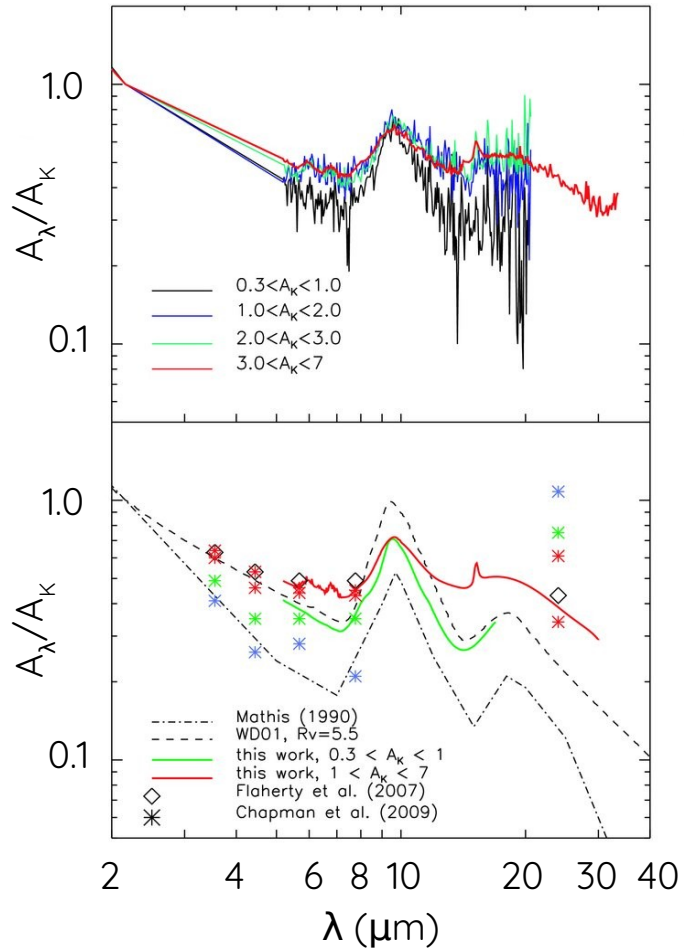
Koehler et al. (2011)



- Aggregates of 8 monomers
monomer \rightarrow 0.1 and 1 μm compact sphere
- Three types of calculations
 - \rightarrow DDA = “exact” method
 - \rightarrow Mie for a sphere of equivalent mass
 - \rightarrow EMT+Mie sphere with same radius of gyration \mathcal{R}_g and $\mathcal{P}_{\text{equivalent}}$
- Significant differences
 - \rightarrow different grain temperatures
 - \rightarrow shifted SEDs
 - \rightarrow mid-IR silicate features \neq size estimates

Example: silicate mid-IR features

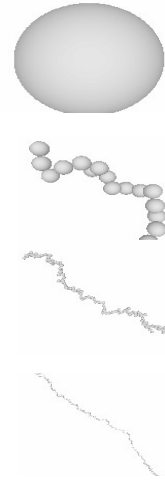
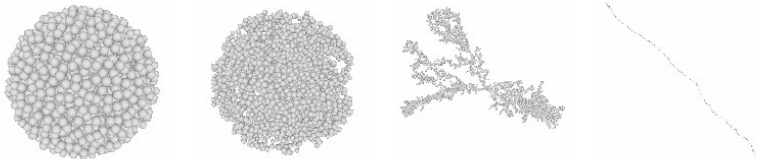
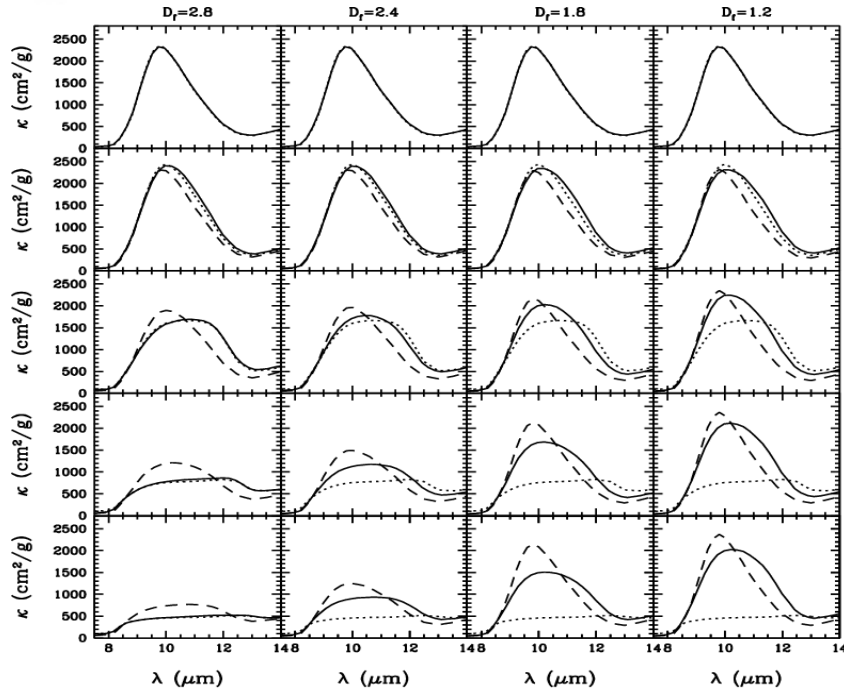
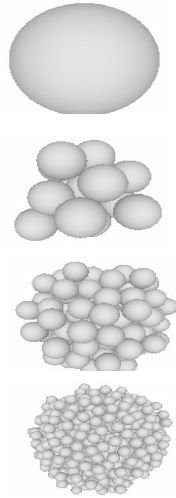
McClure (2009) → observations



- Broader features in dense than diffuse ISM
 - Lower contrast with continuum
- ⇒ significant grain growth ?

Example: silicate mid-IR features

Min et al. (2016) → fractal dimension



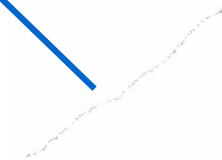
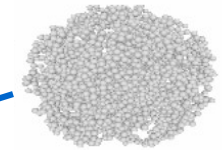
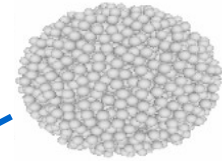
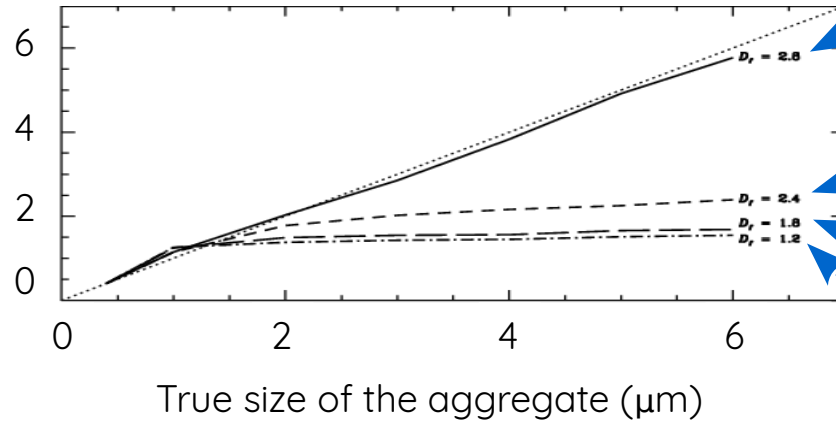
- aggregate
- - volume equivalent compact sphere
- ... equivalent porous sphere
- · - sphere

amorphous "olivine"
monomer radius $a_0 = 0.4 \mu\text{m}$

Example: silicate mid-IR features

Min et al. (2016) → fractal dimension

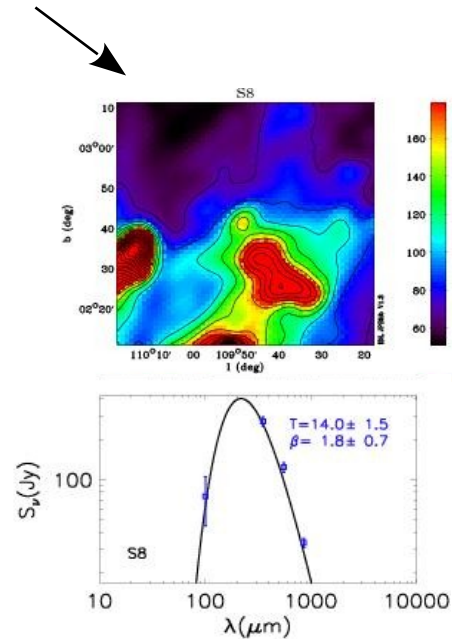
Size when fitting aggregate features
with compact spheres (μm)



sizes UNDERestimated when using compact spheres
sizes OVERestimated when using porous spheres

Many mass estimates based on MBB fits

- Mass estimates based on modified blackbody fits for dense ISM regions
 - ↳ molecular clouds & prestellar cores (e.g. Planck Collaboration 2011 XXII)
 - ↳ young stellar objects & protoplanetary discs (e.g. Busquet et al. 2019)
- Assume a dust opacity at a given wavelength
 - ↳ pb. 1: depends on grain size distribution
 - ↳ pb. 2: depends on grain composition
 - ↳ pb. 3: depends on grain structure
 - ↳ pb. 4: depends on temperature distribution



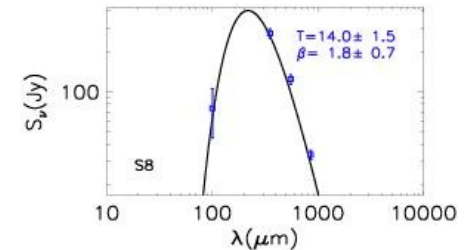
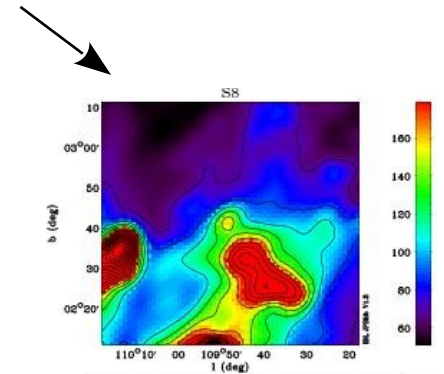
Why is it important to determine $n(a)$?

And not only a_{\max}

- Mass estimates based on modified blackbody fits for dense ISM regions
 - ↳ molecular clouds & prestellar cores (e.g. Planck Collaboration 2011 XXII)
 - ↳ young stellar objects & protoplanetary discs (e.g. Busquet et al. 2019)

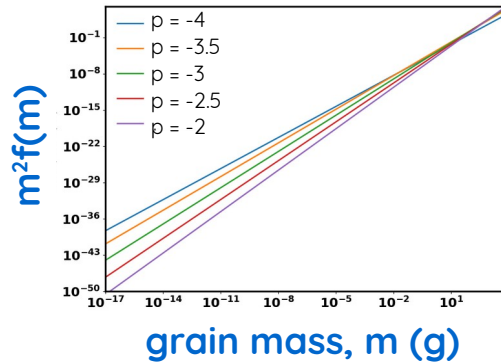
- Assume a dust opacity at a given wavelength
 - ↳ **pb. 1: depends on grain size distribution**
 - ↳ pb. 2: depends on grain composition
 - ↳ pb. 3: depends on grain structure
 - ↳ pb. 4: depends on temperature distribution

- Classical choice for pb. 1: power-law size distribution
 - ↳ Weidenschilling (1997)
 - ↳ Natta & Testi (2004)
 - ↳ Draine (2006)
 - ↳ ...

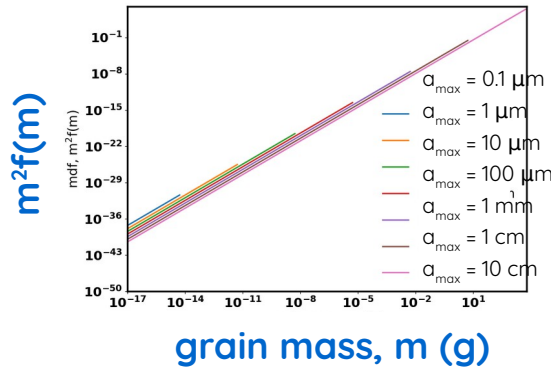


Influence on the dust opacity in the millimetre

Power-law size distribution

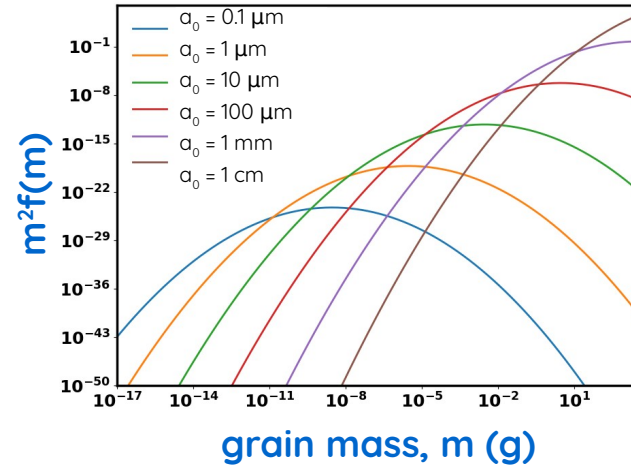


$$\frac{dm}{da} \propto a^p$$



$$\frac{dm}{da} \propto a^{-3.5}$$

Log-normal size distribution



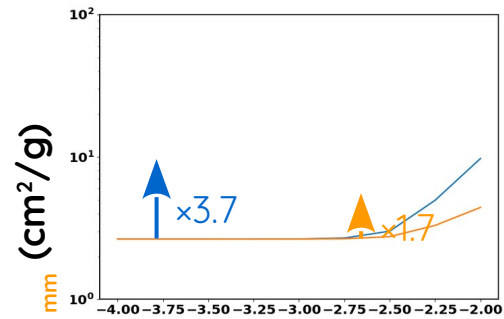
$$\frac{dm}{da} \propto \exp \left\{ -\frac{1}{2} \left[\frac{\ln(a/a_0)}{\sigma} \right]^2 \right\}$$

In all cases: $a_{\min} = 0.01 \mu\text{m}$, $a_{\max} = 10 \text{ cm}$, $M_{\text{gas}}/M_{\text{dust}} = 100$

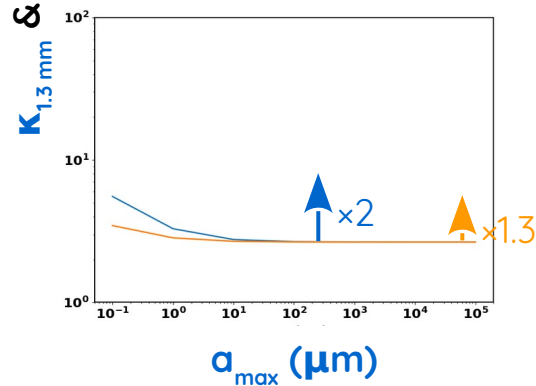
2/3 silicate + 1/3 amorphous carbon + 50% porosity \rightarrow spherical grains

Influence on the dust opacity in the millimetre

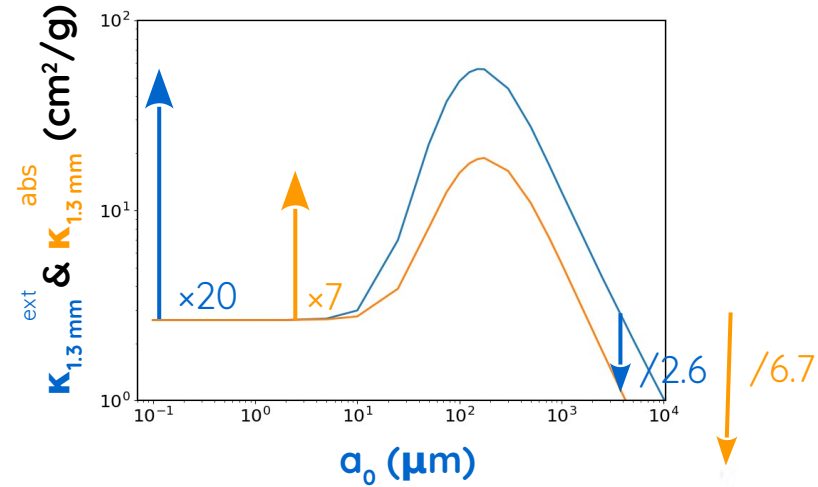
Power-law size distribution



Power-law exponent



Log-normal size distribution



$$\kappa^{\text{ext}} [\text{cm}^2/\text{g}] = \frac{3}{4\rho} \frac{Q_{\text{abs}} + Q_{\text{sca}}}{a}$$

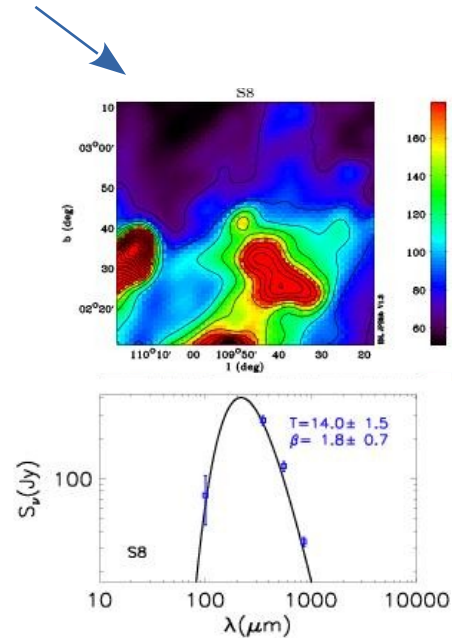
$$\kappa^{\text{abs}} [\text{cm}^2/\text{g}] = \frac{3}{4\rho} \frac{Q_{\text{abs}}}{a}$$

In all cases: $a_{\text{min}} = 0.01 \mu\text{m}$, $a_{\text{max}} = 10 \text{ cm}$, $M_{\text{gas}}/M_{\text{dust}} = 100$

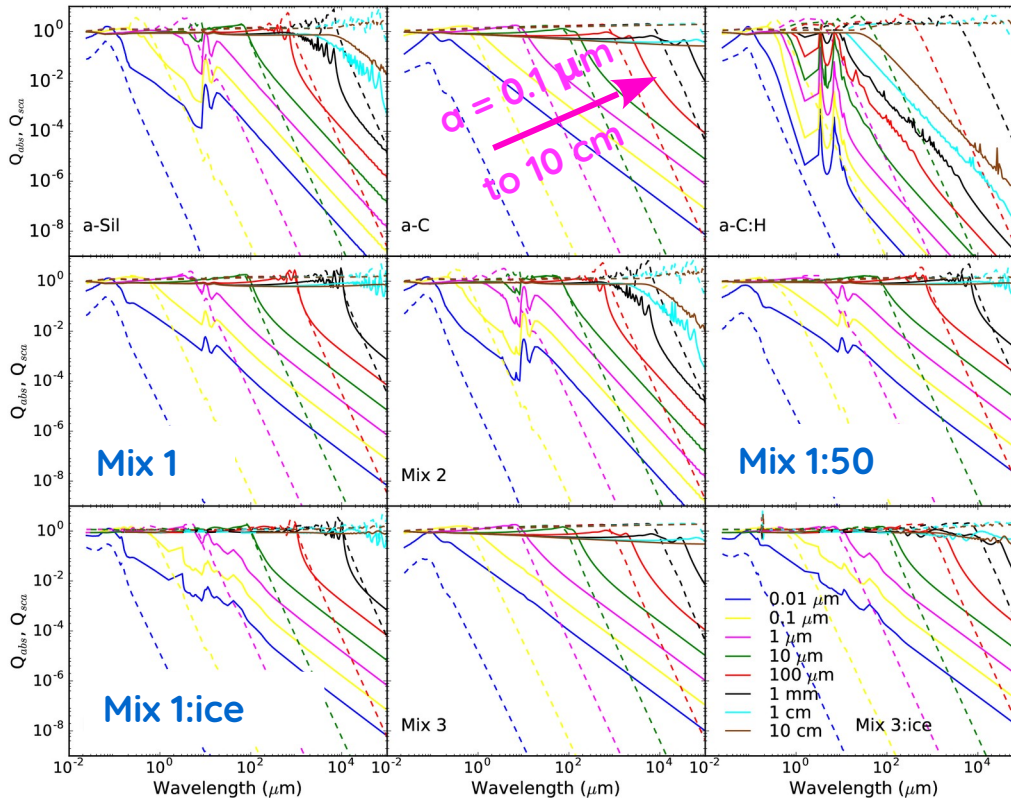
2/3 silicate + 1/3 amorphous carbon + 50% porosity \rightarrow spherical grains

Why is it important to determine the grain composition ? And not only their size

- Mass estimates based on modified blackbody fits for dense ISM regions
 - ↳ molecular clouds & prestellar cores (e.g. Planck Collaboration 2011 XXII)
 - ↳ young stellar objects & protoplanetary discs (e.g. Busquet et al. 2019)
- Assume a dust opacity at a given wavelength
 - ↳ pb. 1: depends on grain size distribution
 - ↳ **pb. 2: depends on grain composition**
 - ↳ pb. 3: depends on grain structure
 - ↳ pb. 4: depends on temperature distribution
- Classical choice for pb. 2: fixed κ value with fixed β
 - ↳ any dust model from the literature



Absorption and scattering efficiencies

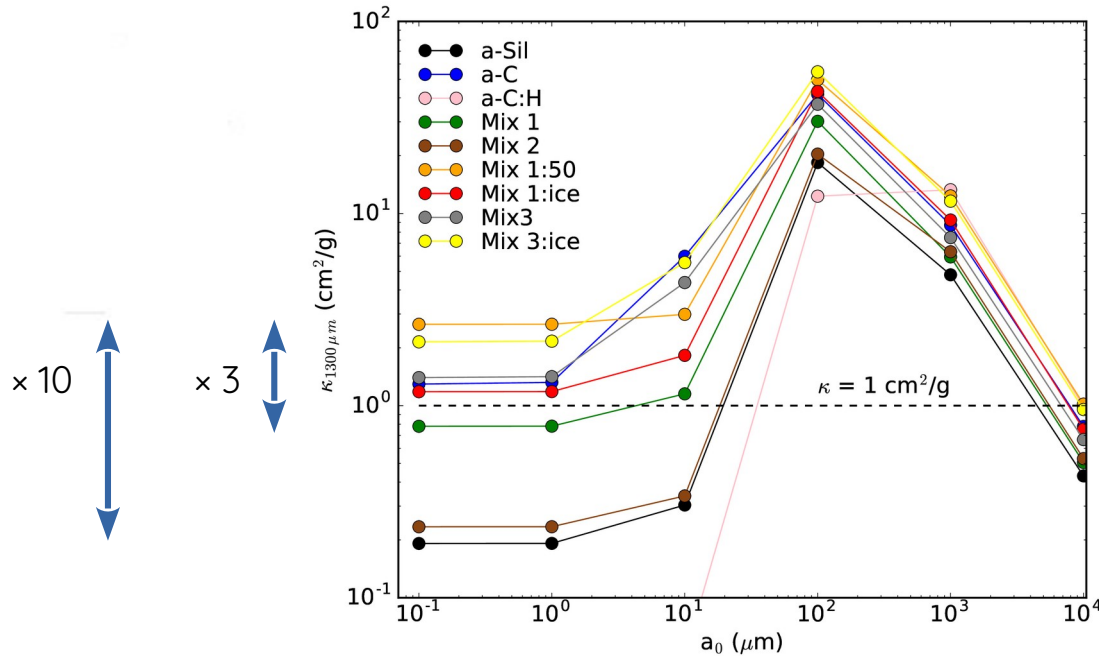


Mix 1 ~ compact AMM
 Mix 1:50 ~ AMM
 Mix 1:ice ~ compact AMMI

Mix 3 & Mix 3:ice ~ Pollack (1994)

α -Sil \rightarrow THEMIS amorphous silicates
 α -C \rightarrow THEMIS $E_g = 0.1$ eV
 α -C:H \rightarrow THEMIS $E_g = 2.5$ eV
 Mix 1 \rightarrow 2/3 α Sil + 1/3 α -C
 Mix 2 \rightarrow 2/3 α Sil + 1/3 α -C:H
 Mix 1:50 \rightarrow porous Mix 1 ~ AMM
 Mix 1:ice \rightarrow Mix 1 with an ice mantle
 Mix 3 \rightarrow 20% α -Sil + 80% α -C
 Mix 3:ice \rightarrow Mix 3 with an ice mantle

Mass absorption coefficients at 1.3 mm



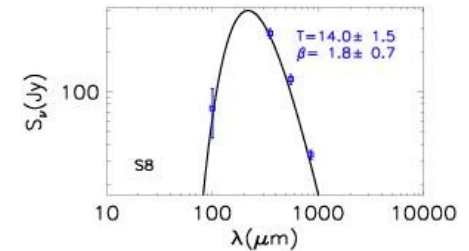
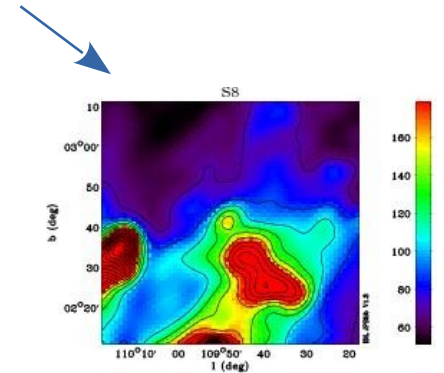
$$\frac{M_{\text{gas}}}{M_{\text{dust}}} = 100$$

$$\frac{dn}{da} \propto \exp \left\{ -\frac{1}{2} \left[\frac{\ln(a/a_0)}{\sigma} \right]^2 \right\}$$

Why is it important to determine the grain composition ?

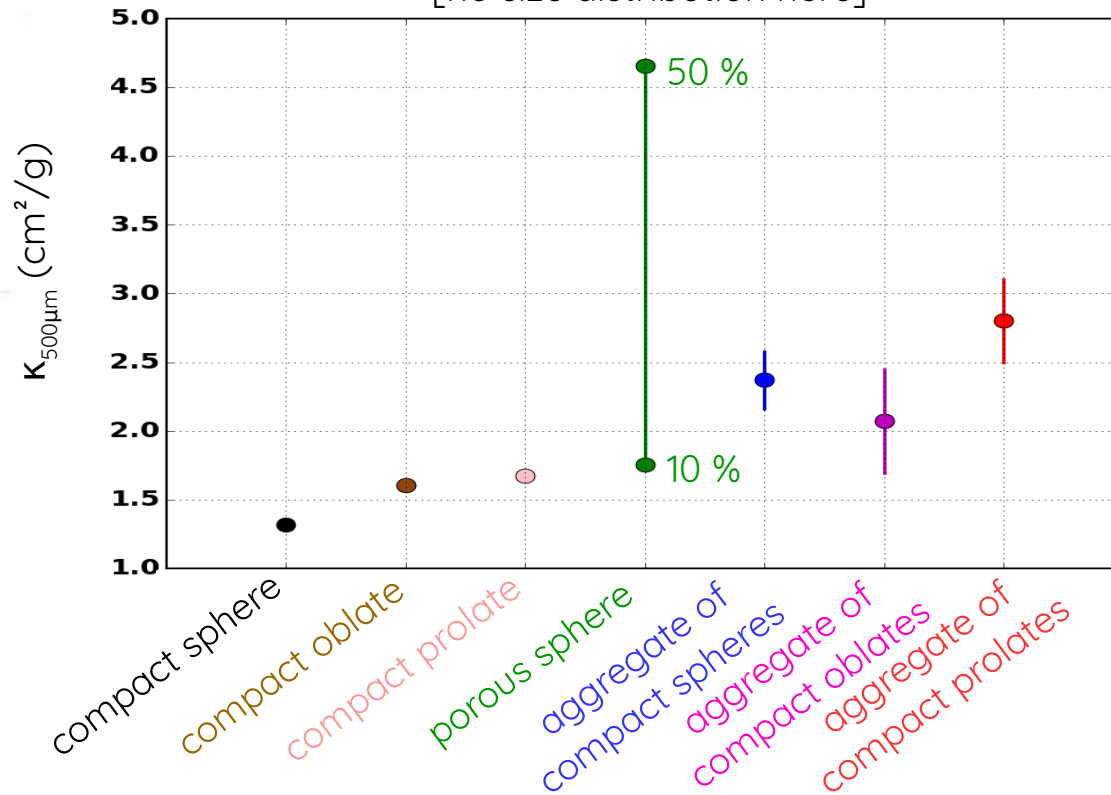
And not only their size and composition

- Mass estimates based on modified blackbody fits for dense ISM regions
 - ↳ molecular clouds & prestellar cores (e.g. Planck Collaboration 2011 XXII)
 - ↳ young stellar objects & protoplanetary discs (e.g. Busquet et al. 2019)
- Assume a dust opacity at a given wavelength
 - ↳ pb. 1: depends on grain size distribution
 - ↳ pb. 2: depends on grain composition
 - ↳ **pb. 3: depends on grain structure**
 - ↳ pb. 4: depends on temperature distribution
- Classical choice for pb. 3
 - ↳ ignore the problem



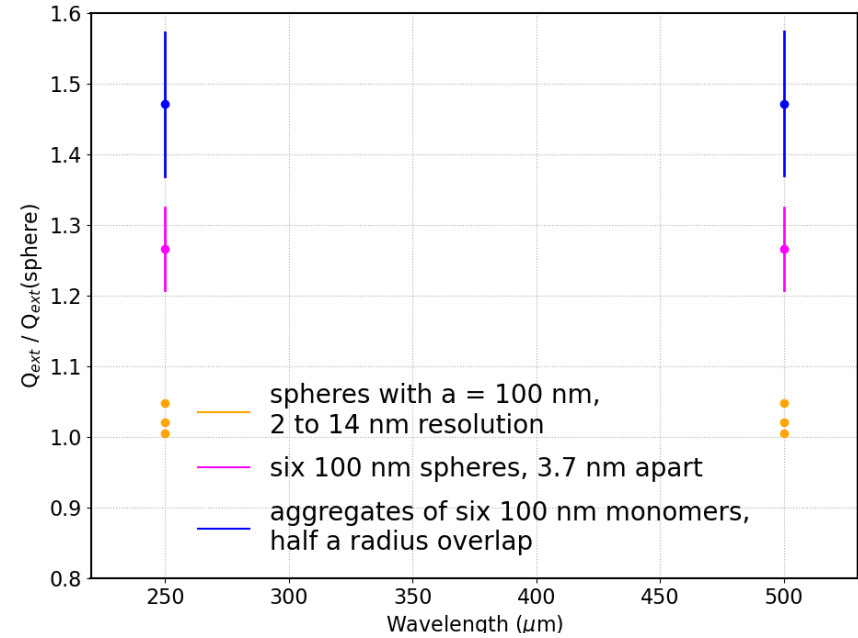
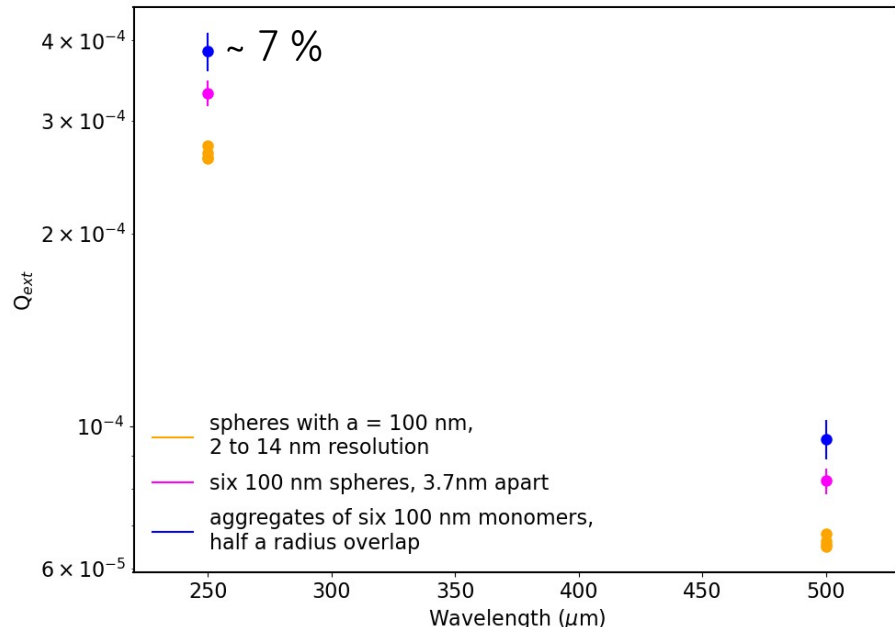
Mass absorption coefficients at 500 μm

100% silicate, mass equivalent size of 0.1 μm
[no size distribution here]



Description of the grain surface

→ completely smooth vs. irregular

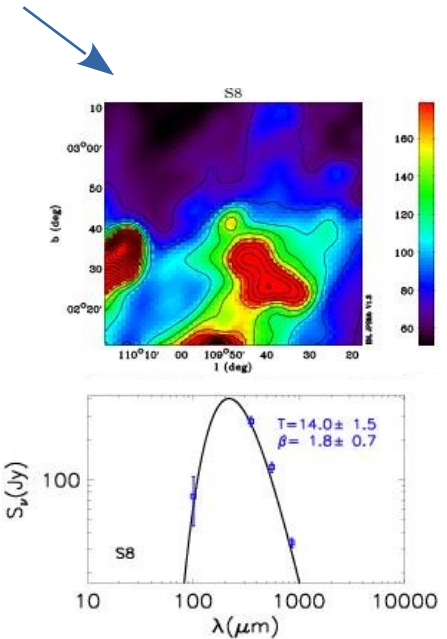


- single grains: increase by $\sim 5\%$ for highly irregular surface
- aggregates: increase by $\sim 20\%$ for large contact area

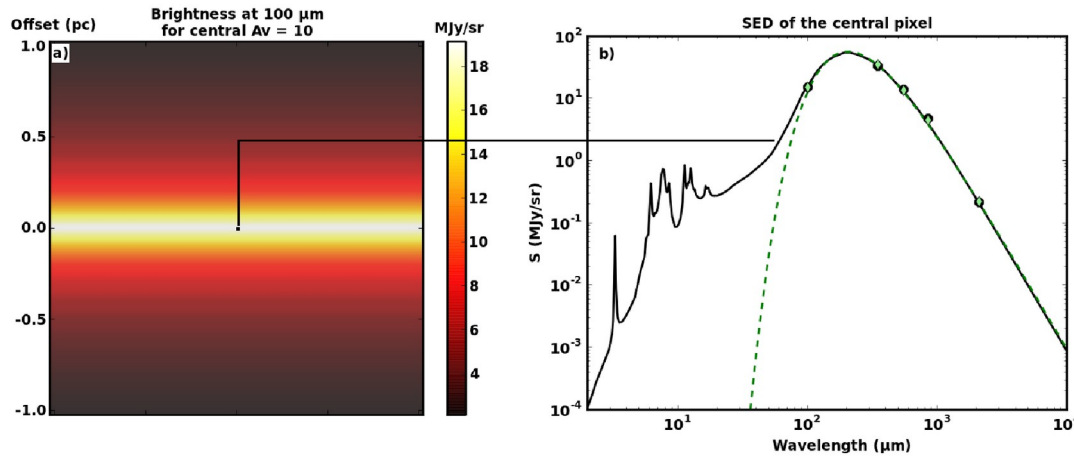
Why is it important to take into account the radiative transfer ?

And not only the dust grain properties

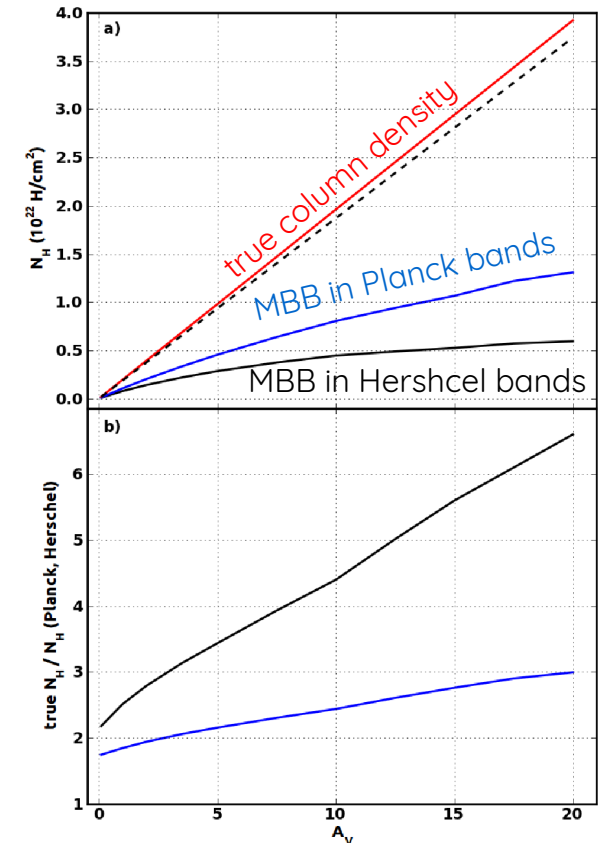
- Mass estimates based on modified blackbody fits for dense ISM regions
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- Assume a dust opacity at a given wavelength
 - ↳ pb. 1: depends on grain size distribution
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 - ↳ pb. 3: depends on grain structure
 - ↳ **pb. 4: depends on temperature distribution**
- Classical choice for pb. 4
 - ↳ depends on the concerned community



Column density as a function of cloud visual extinction



- Cylindrical clouds with $0.1 \leq A_v \leq 20$
- Depending on the dataset, mass can be strongly underestimated when using a MBB



- Dust properties vary both in the diffuse and the dense ISM
- Be careful to always know which dataset was used to define a dust model
→ comparison between different dust models does not always make sense
- Uncertainties in the dust models are probably always larger than uncertainties in your data
- Keep in mind what you are neglecting when fitting your data

Many dust models available in the DustEM numerical tool to calculate dust emission & extinction (polarised or not)
<https://www.ias.u-psud.fr/DUSTEM/>